

# Design Optimization of a Pico Linear Permanent Magnet Generator with Novel Shaped Magnet for Wave Energy Conversion using Finite Element Analysis

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## Abstract

This paper presents the design optimization of a pico linear permanent magnet (PM) generator with novel shaped magnet for wave energy conversion. The finite element analysis (FEA) using time-stepping finite element method has been carried out where the electromagnetic characteristics such as open-circuit magnetic field distribution, magnetic flux density, induced-EMF, and flux linkage are presented. The optimization has been carried out based on the leading dimensions; angle " $\beta$ ",  $T_m/T_p$ , and  $R_m/R_e$ , which have significant influence on the performance of linear PM generator. The optimum values for  $T_m/T_p$ , PM angle  $\beta$  and  $R_m/R_e$  are 0.7,  $80^\circ$  and 0.72 are achieved respectively, which yields maximum efficiency.

**Keywords:** Wave energy, linear generator, finite element analysis, efficiency, copper loss, core loss, optimization, dimensional ratio.

## Introduction

Wave energy has a high seasonal availability and is fuel free, predictable and environment friendly. It is estimated that the potential worldwide wave power resource is 2 TW [1]. Since past decades, various efforts have been accomplished in the field of wind and solar energy generation. Alternatively, wave energy is still on initial stage but offers high potential energy. Marine wave energy is abundant and much consistent than solar and wind energy [2]. Wave energy is also called "blue energy" and has several potential benefits as compared to "brown energy", which is the form of energy achieved from fossil fuels and "green energy" which includes renewable energy sources such as; solar and wind energy [3]. Wave energy has 2-3 kW/m<sup>2</sup> power density as compared to wind and solar that has 0.4-0.6 kW/m<sup>2</sup> and 0.1-0.2 kW/m<sup>2</sup> respectively, while, in terms of power generation, wave energy converters generate maximum 90 % of power as compared to wind and solar that generates maximum 20-30 %, respectively [4]. The wave to mechanical energy conversion encompasses a full cycle as shown in Fig. 1. The primary stage involves conversion of available pneumatic energy of waves into mechanical energy, the secondary stage include an electrical machine which converts mechanical input to electric output, and the tertiary stage is based on signal conditioning which transform the signal into the form required by the grid. Conventional electrical machines are based on rotating generators that include mechanical section

i.e. turbine part, gearbox and hydraulic pump [5-6]. Alternatively, direct-drive linear generator technology is proven efficient in wave energy conversion owing to absence of mechanical interface [7-9].

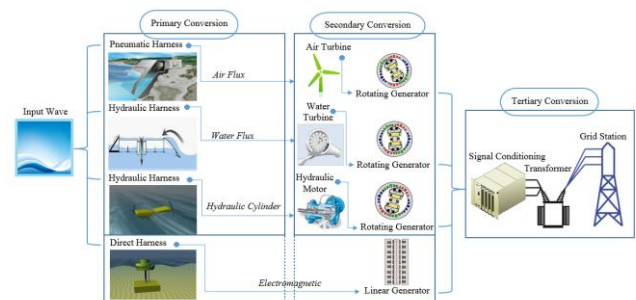


Fig. 1. Wave to electrical conversion cycle

In direct-drive system the moving part i.e. translator relative to stationary part (stator) is directly driven by the wave energy converter (WEC), which simplifies the overall system as shown in Fig. 2. The conventional synchronous generators use electromagnets to obtain magnetic field in the winding that further requires direct current and slip-ring assembly in order to achieve excitation. On the other hand, PM generators do not need a DC supply as an excitation circuit, slip rings and brush assembly [10-12]. PM are solid hard magnetic materials with an extremely large (wide) hysteresis cycle and a recoil permeability of 1.05-1.3 [13].

Variable Reluctance PM (VRPM) machines are recognized as high force density machines [10-11]. The type of these machines is Transverse Flux PM (TFPM) machine and Vernier Hybrid PM (VHPM) machine but unfortunately, difficult construction and low power factor are considerable disadvantages of these machines [14]. The development based on the longitudinal flux PM (LFPM) linear generators are very attractive owing to efficient electromagnetic performance but suffers from unwanted issues such as; high magnetic attraction forces and cogging force [15], [16-18]. Alternatively, air-cored linear PM generators are very attractive in terms of simplicity, lightweight [7-8] and unavailability of unwanted magnetic attraction forces and cogging force [10-11] but have limitations in electromagnetic performance. In past, various developments on air-cored machines [7], [10], [14], [19-20] have been carried out; these developments are based on high rating [7], [10-11], [19],

large-scale [20] and complicated design [10-11]. This research aims to propose and design a linear permanent magnet generator [12] which is simple, with low power rating 100 W and portable i.e. lightweight. This paper presents the modeling and design optimization of simple and lightweight linear PM generator based on trapezoid-shaped permanent magnet for wave energy conversion using finite element software ANSYS “Maxwell”.

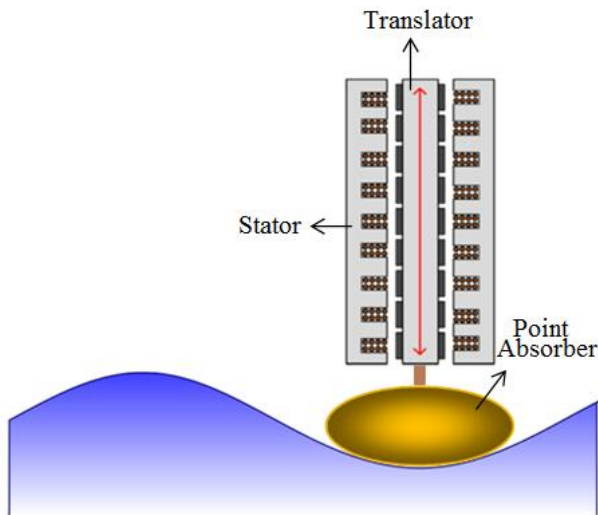


Fig. 2. Direct-drive wave energy conversion system

### Linear Permanent Magnet Generator

The three-dimensional view of proposed linear generator is shown in Fig. 3. The translator is equipped with series of trapezoid-shaped permanent magnets. Neodymium-iron-boron (NdFeB) permanent magnet with the magnetic remanence of 1.14 T is used and quasi-halbach magnetization is employed on account of sinusoidal air-gap distribution [21]. The stator uses full-pitch winding with slot-less configuration which reduces the mass and in turn gives a simple and lightweight design [22].

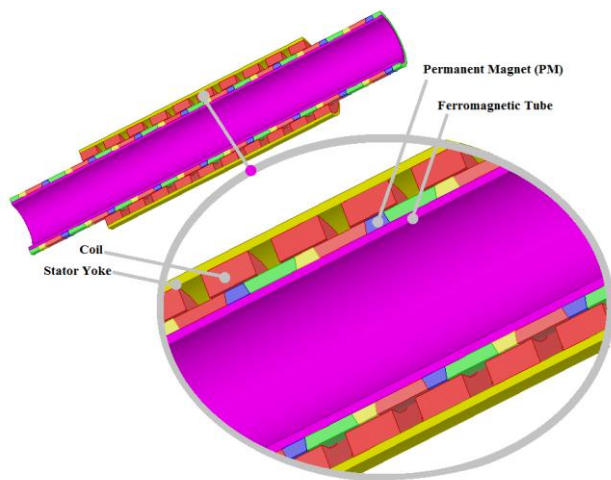
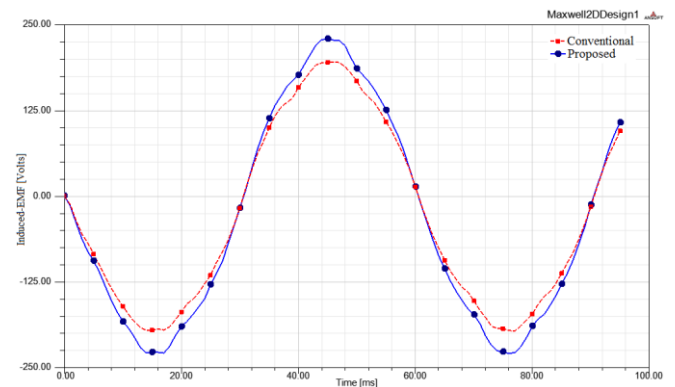


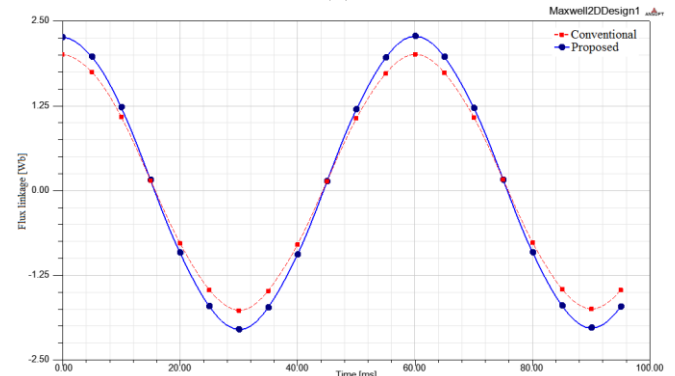
Fig. 3. Three-dimensional view of proposed Linear PM generator

### Finite Element Analysis

FEA has been carried out on conventional linear PM generator with rectangular-shaped magnet. It validates with proposed design and identify that the proposed linear generator produces superior and higher electromagnetic performance as compared to conventional linear generator [23-27]. The axis-symmetrical cylindrical coordinate system is adopted. The boundary conditions are applied to all regions and the magnetization has been assigned to all permanent magnets [28]. Fig. 4. presents the comparison of induced-EMF and flux linkage for conventional [27] and proposed linear generator. It will be seen that, the proposed linear generator has higher performance as compared to conventional linear generator [27].



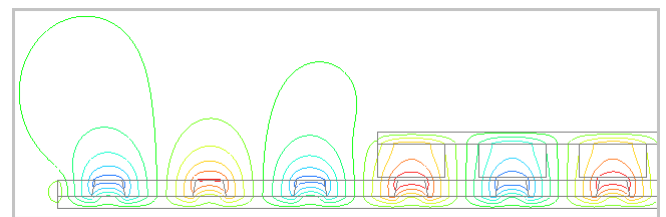
(a)



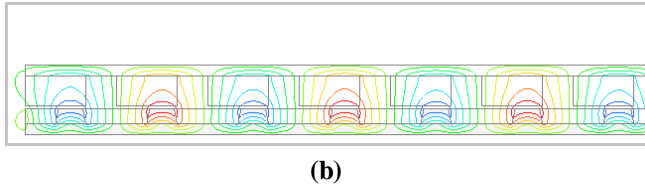
(b)

Fig. 4. Comparison of conventional and proposed design  
(a) Induced-EMF (b) Flux linkage

The finite element predicted open-circuit flux distribution at zero and maximum displacement  $Z_d$  ( $Z_d=0$ ) are shown in Fig. 5. It will be seen that flux distribution is uniform and forms smooth linkage between translator and stator.

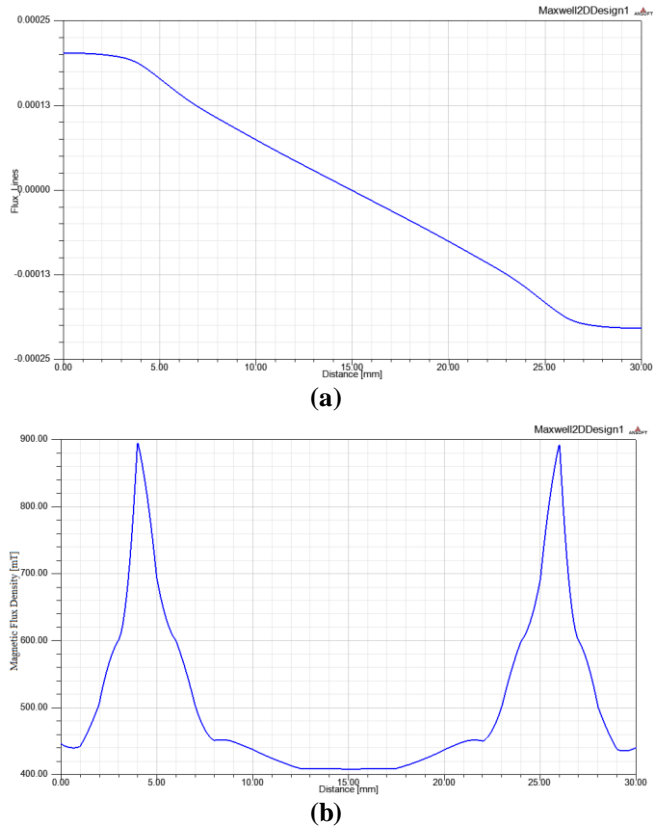


(a)



**Fig. 5. Open-circuit flux distribution between translator and stator at (a) ( $Z_d$  at zero displacement) (b) ( $Z_d$  at maximum displacement)**

The air-gap is the mechanical clearance between translator and stator, the magnetic flux density and flux line for one pole-pitch at zero displacement are shown in Fig. 6.



**Fig. 6. Magnetic flux density (a) magnetic flux lines (b) in air-gap between translator and stator**

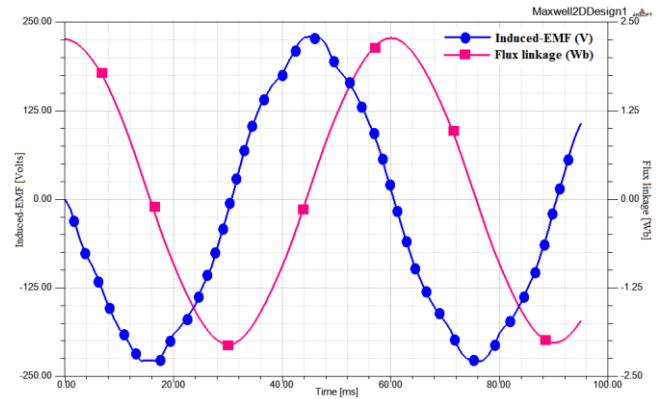
Transient mode is a time-varying analysis and it is also called “on-motion” analysis. The translator is fixed on the center with respect to stator and is reciprocated with the velocity of 1 m/s. The stop time and time step is 30 ms and 1 ms, respectively with the step size of 5 ms. The RMS Induced-EMF generated in stator winding [29] can be written as;

$$E = \frac{2\pi}{\sqrt{2}} f N_{ph} \phi_m \quad (1)$$

where  $E$  is the induced-EMF,  $f$  is electrical frequency,  $N_{ph}$  is the number of coil turns per phase and  $\phi_m$  flux linked by winding.

The induced-EMF and flux linkage in the winding of stator is shown in Fig. 7. It will be seen that, the resultant waveform is

sinusoidal [29] which in turn reduces the requirement of signal conditioning portion.



**Fig. 7. Induced-EMF and flux linkage in coil of stator's winding**

### Efficiency Analysis

The efficiency of the electrical machine is the essential part that is to be taken into account under the design optimization [30]. The efficiency has been analysed as follows [31];

$$\eta = \frac{P_{out}}{P_{out} + P_{cu} + P_{fe}} \quad (2)$$

where  $P_{out}$ ,  $P_{cu}$ , and  $P_{fe}$  is output power, copper loss and iron loss, respectively.

Copper loss can be determined as follows [32];

$$P_{cu} = I^2 R \quad (3)$$

where  $I$  and  $R$  is rms current and winding resistance, respectively.

The core loss or iron loss of the linear permanent magnet generator is composed of three different components [33]; hysteresis loss, classical eddy current loss, and excessive loss. Collectively, the total core loss [34] can be expressed as;

$$P_{fe} = \Sigma(P_{hi} + P_{ci} + P_{ei}) \quad (4)$$

where  $P_{hi}$ ,  $P_{ci}$  and  $P_{ei}$  is hysteresis loss, classical eddy current loss and excessive loss, respectively. Using flux density waveform [33-34], these components can be written as;

$$P_{hi} = \kappa_h f B_m^\alpha \quad (5)$$

$$P_{ci} = \frac{2\pi\sigma d^2 f^2}{12\delta} \int_{2\pi} \left( \frac{dB}{d\theta_e} \right)^2 d\theta_e \quad (6)$$

$$P_{ei} = \sqrt{2\pi} \kappa_e f^{\frac{3}{2}} \int_{2\pi} \left| \frac{dB}{d\theta_e} \right|^{\frac{3}{2}} d\theta_e \quad (7)$$

where  $f$ ,  $B_m^\alpha$  and  $\theta_e$  are the frequency, peak flux density and electrical degree, respectively, and  $\sigma$ ,  $\delta$  and  $d$  are the electrical conductivity, mass density and lamination thickness, respectively. The coefficients  $\kappa_h$ ,  $\alpha$  and  $\kappa_e$  associated with hysteresis and excess loss component can be determined from manufacturer's data sheet.

### Design Optimization

The objective of optimization is to maximize efficiency and minimize the total losses [35]. In order to achieve maximum value of efficiency, the leading design parameters which have significant influence on the performance of linear PM generator are optimized. The main leading design parameters

are; permanent magnet angle " $\beta$ ", ratio of  $T_{mr}/T_p$  and ratio of  $R_m/R_e$ . The optimization of design parameters is set to constant output power when varying " $\beta$ ",  $T_{mr}/T_p$ , and  $R_m/R_e$ . This is due to give equal or fair process of optimization [36]. The schematic diagram of linear PM generator with geometric parameters is presented in Fig. 8. and their dimension is listed in Table I;

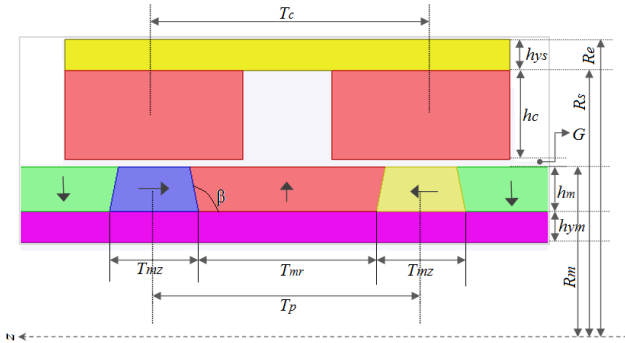


Fig. 8. Schematic diagram of linear PM generator

TABLE I. Dimension of design parameters

Parameter	Value
Rated Power, $P_{out}$	100 W
Length of radially magnetized magnet, $T_{mr}$	20 mm
Length of axially magnetized magnet, $T_{mz}$	10 mm
Magnet height, $h_m$	5 mm
Pole-pitch, $T_p$	30 mm
Outer radius of stator core, $R_e$	52.8 mm
Radial thickness of ferromagnetic tube, $h_{ym}$	3.5 mm
Stator yoke height, $h_s$	3.5 mm
Reciprocating velocity, $v$	1 m/s
Air-gap length, $G$	0.8 mm
Magnetic Remanence, $B$	1.14 T

#### A. Influence of angle ( $\beta$ )

The translator of linear generator is equipped with trapezoid-shaped permanent magnet, which is highly influenced by the angle of permanent magnet ( $\beta$ ). The variation of angle ( $\beta$ ) is worthwhile because it gives rise to the flux-linkage and in turn increases induced-EMF but after optimal value it diminishes the performance owing to drop in flux-linkage. The output power is set constant when varying the angle as shown in Fig. 9. Fig. 10 shows the angle of permanent magnet is optimized for various degrees. It will be seen that, on  $80^\circ$  the maximum induced-EMF is achieved.

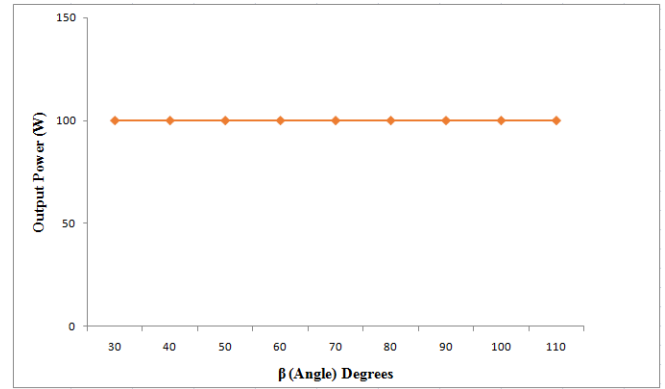


Fig. 9. The output power versus variation of angle  $\beta$

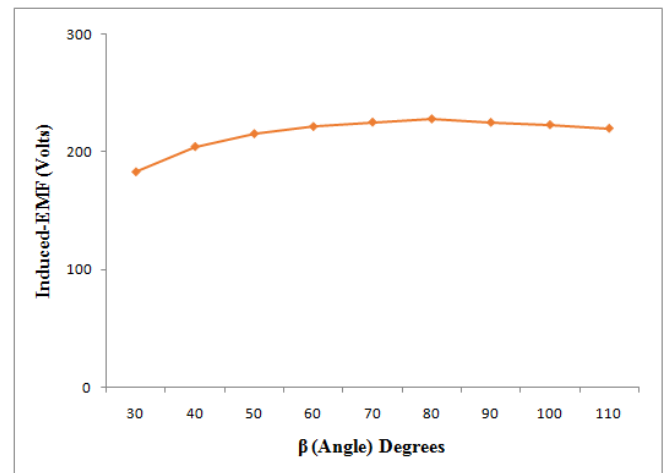


Fig. 10. Influence of angle  $\beta$  on induced-EMF

Similarly, the efficiency of linear generator is analyzed on various degrees of permanent magnet angle  $\beta$ , which exhibits higher value on  $80^\circ$  as shown in Fig. 11.

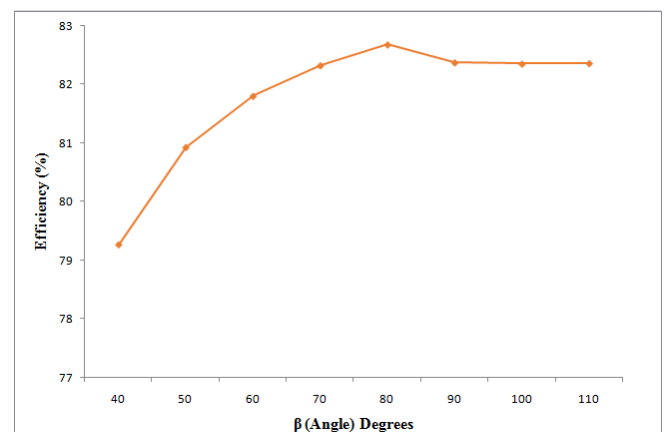
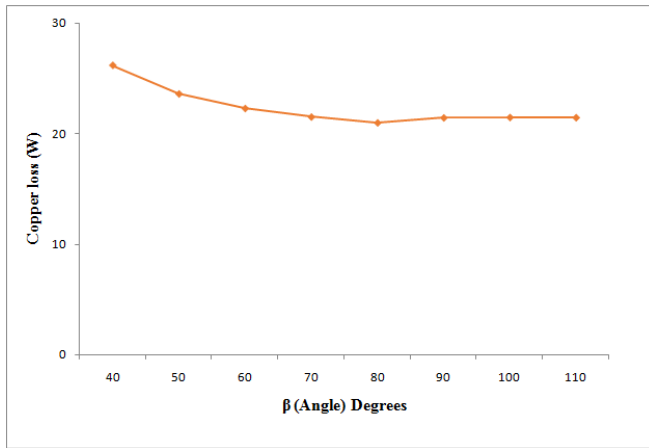


Fig. 11. Influence of angle  $\beta$  on efficiency

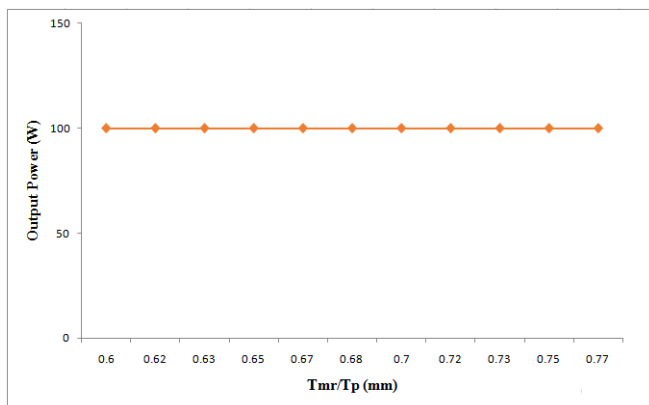
The same trend is analyzed for copper loss, the copper loss has minimum value on  $80^\circ$  (degrees) as shown in Fig. 12.



**Fig. 12. Influence of angle  $\beta$  on copper loss**

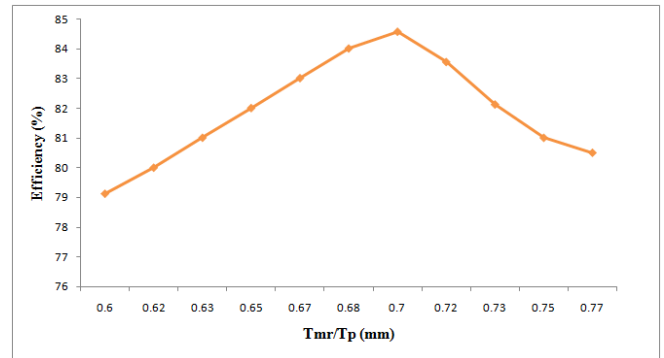
### B. Influence of $T_{mr}/T_p$

The optimization is carried out by keeping output power to a constant value by adjusting the magnitude of current [17-18] as shown in Fig. 13.  $T_{mr}/T_p$  is the called “pole-width ratio” [37-38], it is very significant due to it affects the maximum flux-linkage between coil and PM. The thickness and pole-pitch for permanent magnet is kept constant during optimization.



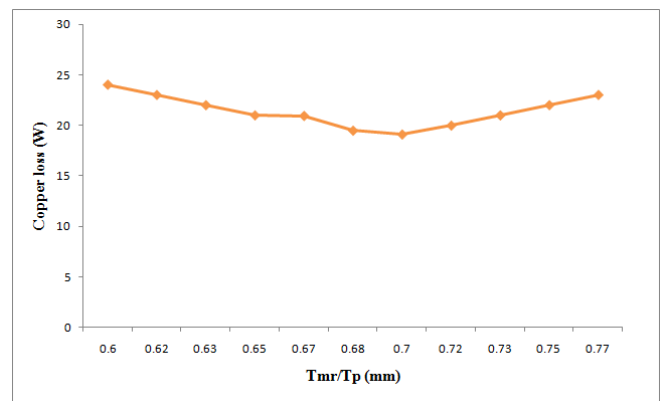
**Fig. 13. The output power versus variation of  $T_{mr}/T_p$**

Fig. 14 shows the variation of the efficiency with  $T_{mr}/T_p$  at optimal value of  $\beta = 80^\circ$ . It will be seen that, the optimal ratio occurs at  $T_{mr}/T_p = 0.70$ , which gives maximum efficiency and afterwards the flux linkage causes saturation which in turn diminish the efficiency.



**Fig. 14. Influence of  $T_{mr}/T_p$  on the efficiency of linear permanent magnet generator**

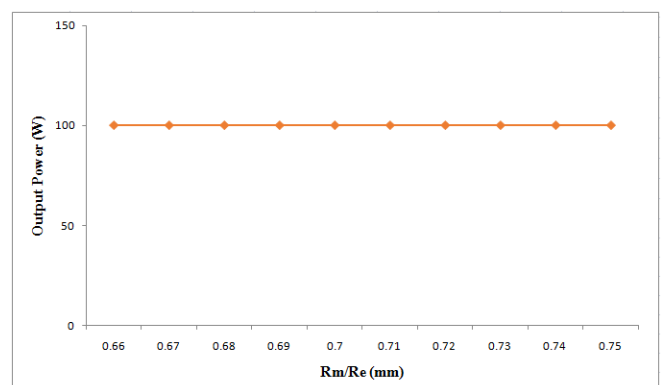
Fig. 15 shows the influence of  $T_{mr}/T_p$  on the copper loss of the linear permanent magnet generator. It will be seen that, at 0.70 the copper loss has minimum value.



**Fig. 15. Influence of  $T_{mr}/T_p$  ratio on copper loss**

### C. Influence of $R_m/R_e$

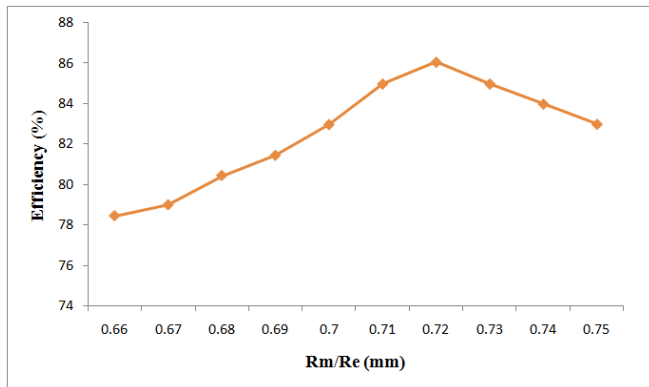
The  $R_m/R_e$  ratio is called “split ratio”, it is an optimal balance between magnetic and electrical loading [39-40]. It is very significant part because its variation determines the maximum efficiency and minimum losses. Likewise, the output power is kept constant by adjusting the magnitude of current as shown in Fig. 16. The outer diameter of stator is kept constant when varying radius of outer diameter of translator.



**Fig. 16. The output power versus variation of  $R_m/R_e$**

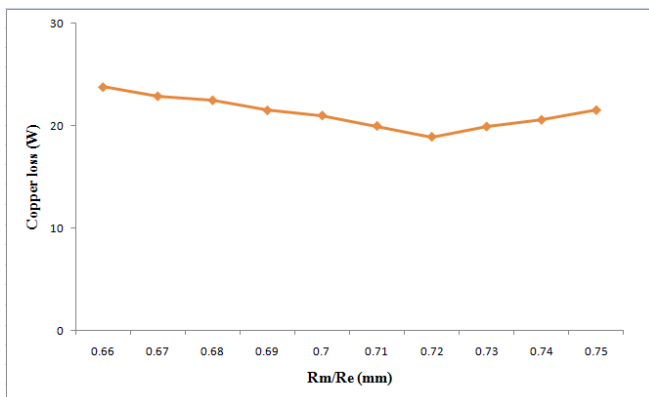


Fig. 17 shows the variation of the efficiency as a function of  $R_m/R_e$ . It is seen that, the optimal ratio is  $R_m/R_e = 0.72$ , which gives maximum efficiency.



**Fig. 17. Influence of  $R_m/R_e$  on the efficiency of linear permanent magnet generator**

Fig. 18 shows the influence of  $R_m/R_e$  on the copper loss of the linear permanent magnet generator. It will be seen that, the minimum value on which copper loss is minimum occurs at 0.72.



**Fig. 18. Influence of  $R_m/R_e$  ratio on copper loss**

## Conclusion

The linear PM generator with trapezoid-shaped permanent magnet and its electromagnetic characteristics; open-circuit magnetic flux distribution, induced-EMF, and flux linkage are presented. The characteristics show that the linear PM with trapezoidal shape magnet has better performance than the linear PM generator with rectangular shape magnet. The optimization has been carried out for highest efficiency and the influence of leading dimensional parameters; permanent magnet angle  $\beta$ , ratio of  $T_m/T_p$  and ratio of  $R_m/R_e$  are analyzed. The proposed design will be fabricated and tested in order to validate the results.

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## References

- [1] J. Falnes, "A review of wave-energy extraction," *Marine Structures*, vol. 20, pp. 185–201, October 2007.
- [2] S. H. Salter, "Wave power," *Nature*, vol. 249, pp. 720–724, 1974.
- [3] J. Tollefson, "Blue energy: after years in the doldrums, the quest to harvest energy from the oceans is gathering speed," *Nature*, vol. 508, pp. 302–304, 2014.
- [4] I. López, J. Andreu, S. Ceballos, I. M. d. Alegría, and I. Kortabarria, "Review of wave energy technologies and the necessary power-equipment," *Renewable and Sustainable Energy Reviews*, vol. 27, pp. 413–434, 2013.
- [5] A. H. Memon, T. b. Ibrahim, and P. Nallagownden, "Modelling and analysis of linear permanent magnet generator for wave energy conversion using finite element method," *Applied Mechanics and Materials*, vol. 785, pp. 258–262, 2015.
- [6] A. H. Memon, T. b. Ibrahim, and P. Nallagownden, "Comparative study of linear permanent magnet generator with different shape of permanent magnet for wave energy conversion," in *Proceedings International Conference on Electrical Power Engineering and Applications*, Langkawi, Malaysia, 2014.
- [7] N. Hodgins, O. Keysan, A. S. McDonald, and M. A. Mueller, "Design and testing of a linear generator for wave energy applications," *IEEE Transactions on Industrial Electronics*, vol. 59, pp. 2094–2103, 2012.
- [8] A. H. Memon, T. b. Ibrahim, and P. Nallagownden, "Modeling and analysis of linear permanent magnet generator for wave energy conversion using finite element method," in *Proceedings 9th International Power Engineering and Optimization Conference*, Melaka, Malaysia, 2015.
- [9] H. Polinder, B. C. Mecrow, A. G. Jack, P. G. Dickinson, and M. A. Mueller, "Conventional and TFPM linear generators for direct-drive wave energy conversion," *IEEE Transactions on Energy Conversion*, vol. 20, pp. 260–267, 2005.
- [10] R. Vermaak and M. J. Kamper, "Design of a novel air-cored permanent magnet linear generator for wave energy conversion," in *Proceedings International Conference on Electrical Machines*, Rome, Italy, 2010, pp. 1–6.
- [11] R. Vermaak and M. J. Kamper, "Design aspects of a novel topology air-cored permanent magnet linear generator for direct drive wave energy converters," *IEEE Transactions on Industrial Electronics*, vol. 59, pp. 2104–2115, May 2012.

- [12] A. H. Memon, T. b. Ibrahim, and P. Nallagowden, "Portable and pico-scale linear generator for wave energy conversion," in *proceedings 5th International Conference on Intelligent and Advanced Systems*, Kuala Lumpur, 2014.
- [13] A. H. Memon, T. b. Ibrahim, and P. Nallagowden, "Comparative study of linear permanent magnet generator with different shape of permanent magnet for wave energy conversion," *Applied Mechanics and Materials*, vol. 793, pp. 197-201, 2015.
- [14] M. A. Mueller and N. J. Baker, "Direct drive power take-off for offshore marine energy converters," in *Proc. Inst. Mech. Eng. A, J. Power Energy*, vol. 219, pp. 223-234, May 2005.
- [15] O. Danielsson, M. Leijon, and E. Sjøstedt, "Detailed study of the magnetic circuit in a longitudinal flux permanent-magnet synchronous linear generator," *IEEE Transactions on Magnetics*, vol. 41, pp. 2490-2495, 2005.
- [16] K. Nilsson, O. Danielsson, and M. Leijon, "Electromagnetic forces in the air gap of a permanent magnet linear generator at no load," *Journal of Applied Physics*, vol. 99, pp.-, 2006.
- [17] N. M. Kimoulakis, A. G. Kladas, and J. A. Tegopoulos, "Power generation optimization from sea waves by using a permanent magnet linear generator drive," *IEEE Transactions on Magnetics*, vol. 44, pp. 1530-1533, 2008.
- [18] M. A. Mueller, A. S. McDonald, and D. E. Macpherson, "Structural analysis of low-speed axial-flux permanent-magnet machines," *IEE Proceedings on Electric Power Applications*, vol. 152, pp. 1417-1426, November 2005.
- [19] N. J. Baker, M. A. Mueller, and E. Spooner, "Permanent magnet air-cored tubular linear generator for marine energy converters," in *Second International Conference on Power Electronics, Machines and Drives*, Edinburgh, UK, 2004, pp. 862-867.
- [20] P. C. J. Clifton, R. A. McMahon, and H.-P. Kelly, "Design and commissioning of a 30 kW direct drive wave generator," in *5th IET International Conference on Power Electronics, Machines and Drives (PEMD 2010)*, Brighton, UK, 19-21 April 2010, pp. 1-6.
- [21] J. Wang, G. W. Jewell, and D. Howe, "A general framework for the analysis and design of tubular linear permanent magnet machines,," *IEEE Transactions on Magnetics*, vol. 35, pp. 1986-2000, May 1999.
- [22] M. Mueller, A. McDonald, K. Ochije, and J. Jeffrey, "A novel lightweight permanent magnet generator for direct drive power take off in marine renewable energy converters," in *Proceedings 7th European Wave and Tidal Energy Conference*, Porto, Portugal, Sep 2007.
- [23] Y. M. Desai, *Finite element method with applications in engineering*: Pearson Education India, 2011.
- [24] G. Ramamurty, *Applied finite element analysis*: I. K. International Pvt Ltd, Jul 1, 2010.
- [25] X.-S. Yang, *A first course in finite element analysis*: Luniver Press, 2007.
- [26] N. Bianchi, *Electrical machine analysis using finite elements*: CRC Press, Jun 17, 2005
- [27] C.-T. Liu, C.-L. Lin, C.-C. Hwang, and C.-H. Tu, "Compact model of a slotless tubular linear generator for renewable energy performance assessments," *IEEE Transactions on Magnetics*, vol. 46, pp. 1467-1470, 2010.
- [28] J. Wang, G. W. Jewell, and D. Howe, "Design optimisation and comparison of tubular permanent magnet machine topologies," *IEE Proceedings-Electric Power Applications*, vol. 148, pp. 456-464, 2001.
- [29] R. Vermaak, "Development of a novel air-cored permanent magnet linear generator for direct drive ocean wave energy converters," Department of Electrical and Electronic Engineering, Faculty of Engineering, Stellenbosch University, March 2013.
- [30] T. Ibrahim, J. Wang, D. Howe, and N. M. Nor, "Design and optimisation of a moving-iron linear permanent magnet motor for reciprocating compressors using finite element analysis," *International Journal of Electrical & Computer Sciences*, vol. 10, pp. 78-84, 2010.
- [31] R. E. Clark, D. S. Smith, P. H. Mellor, and D. Howe, "Design optimization of moving-magnet actuators for reciprocating electro-mechanical systems," *IEEE Transactions on Magnetics*, vol. 31, pp. 3746-48, Nov. 1995.
- [32] B. D. Cullity and C. D. Graham, *Introduction to magnetic materials*, Second ed.: Wiley-IEEE Press, November 2008.
- [33] Y. Amara, J. Wang, and D. Howe, "Stator iron loss of tubular permanent-magnet machines," *IEEE Transactions on Industry Applications*, vol. 41, pp. 989-995, 2005.
- [34] J. Wang, T. Ibrahim, and D. Howe, "Prediction and measurement of iron loss in a short-stroke, single-phase, tubular permanent magnet machine," *IEEE Transactions on Magnetics*, vol. 46, pp. 1315-1318, June 2010.
- [35] J. Wang, D. Howe, and Z. Lin, "Design optimization of short-stroke single-phase tubular permanent-magnet motor for refrigeration applications," *IEEE Transactions on Industrial Electronics*, vol. 57, pp. 327-334, 2010.
- [36] J. Wang and D. Howe, "Design optimization of radially magnetized, iron-cored, tubular permanent-magnet machines and drive systems," *IEEE Transactions on Magnetics*, vol. 40, pp. 3262-3277, 2004.
- [37] W. Min, J. T. Chen, Z. Q. Zhu, Y. Zhu, and G. H. Duan, "Optimization of linear flux switching permanent magnet motor," in *Proceedings IEEE Conference on Vehicle Power and Propulsion Conference*, Lille, 1-3 Sept. 2010.

- [38] R. C. Crozier, "Optimisation and comparison of integrated models of direct-drive linear machines for wave energy conversion," Doctor of Philosophy, University of Edinburgh, United Kingdom, 2013.
- [39] W. Min, J. T. Chen, Z. Q. Zhu, Y. Zhu, M. Zhang, and G. H. Duan, "Optimization and comparison of novel E-core and C-core linear switched flux PM machines," *IEEE Transactions on Magnetics*, vol. 47, pp. 2134-2141, 2011.
- [40] J. Wang, T. Ibrahim, and D. Howe, "Design optimization of short-stroke, single phase tubular permanent magnet motor for refrigeration applications," in *Proceedings 18th International Conference on Electrical Machines*, Vilamoura, 6-9 Sept. 2008, pp. 1-6.