

Analysis of Elastic Scattering of α Particles on $^{70, 72, 74, 76}\text{Ge}$ targets at $E_{\text{Lab}}=25\text{MeV}$

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Abstract

The elastic scatterings of α particles on $^{70, 72, 74, 76}\text{Ge}$ targets at $E_{\text{Lab}} = 25$ MeV have been analyzed by using combination between McIntyre model and Regge pole model which is based on concept of strong absorption parameterization of the scattering matrix elements, by trying to fit the experiment data of elastic scattering. The calculated elastic differential cross sections show agreement with the experimental data, seven parameters extract from models employed as fixed entries in the fitting process for forward angle and backward angle of angular distribution.

When increase in the size of target ion the interaction radius and total reaction cross-section are found increasing, parameters are obtained for colliding nuclei together for all reaction cross sections.

INTRODUCTION

The elastic scattering data is used to explain of heavy-ion one of the important researches in nuclear physics. The theoretical models have been used to analyze the experimental data. A phenomenological model based on the diffraction phenomenon its can analyze experimental data of elastic scattering of heavy nuclear ions in terms of the asymptotic properties of the scattered wave function.

In many nuclear scattering the incident particle is strongly absorbed by entering the target nucleus, Using strong absorption conditions. The experimental data can be explained without any knowledge about the details of the absorption process. This allowed for developing proper for both the amplitude and phase of scattering wave function.[1-3]

This work propose to analyze the experimental data of angular distribution for elastic scattering of α -particles from $^{70, 72, 74, 76}\text{Ge}$, at laboratory energy equal 25MeV using the McIntyre plus Regge models. The analysis will be start the numerical method based on parameterizations of scattering matrix elements and used by the strong absorption model (SAM). This analysis will explain the diffractive condition, and then the parameters and quantities are extracted Such as the grazing angular momentum l_g , diffusivity, etc (1-3)

THEORY

The amplitude $f(\theta)$ as a function as partial wave expansion for elastic scattering expressed by:

$$f(\theta) = \frac{1}{ik} \sum_{\ell=0}^{\infty} (2\ell + 1) [S_{\ell} - 1] P_{\ell}(\cos \theta). \quad (1)$$

S_{ℓ} is the complex amplitude of the ℓ th scattered partial wave, $P_{\ell}(\cos\theta)$ is the Legendre polynomial of order ℓ and k is the wave number. The scattering matrix amplitude is express by:

$$S_{\ell} = \eta_{\ell} e^{2i\delta_{\ell}}. \quad (2)$$

The Coulomb phase shifts are given by the exact solution of the Rutherford scattering problem:

$$\sigma_{\ell} = \arg \Gamma(\ell + 1 + i\eta). \quad (3)$$

the semi-classical strong absorption model has the sharp cutoff conditions (1,3):

$$\begin{aligned} \eta_{\ell} = 0 \quad S_{\ell} = 0 & \quad \text{if } \ell \leq l_g \\ \eta_{\ell} = 1 \quad S_{\ell} = e^{2i\sigma_{\ell}} & \quad \text{if } \ell > l_g \end{aligned} \quad (4)$$

Here η_{ℓ} is called the reflection coefficient of the outgoing ℓ th partial wave determined by the boundary conditions at the nuclear surface. This means that waves up to the grazing angular momentum l_g are completely absorbed,

The sum of radii R of the projectile R_p , and target nuclei R_T

This strong interaction radius has been defined :

$$R = r_0 (A_p^{1/3} + A_T^{1/3}) \quad (5)$$

Regge-pole factor expressed as:

$$S(\ell) = [1 + e^{-i\alpha} e^{(\ell_g - \ell)/\Delta}]^{-1} \left[1 + \frac{\ell - \ell_0 - iz(\ell)}{\ell - \ell_0 - ip(\ell)/2} \right],$$

Or (6)

$$S(\ell) = [1 + e^{-i\alpha} e^{(\ell_g - \ell)/\Delta}]^{-1} \left[1 + \frac{iD(\ell)}{\ell - \ell_0 - i\Gamma(\ell)/2} \right].$$

The $z(\ell)$ and $p(\ell)$ functions, in equation, represent the Regge zero and Regge pole at a complex ℓ (1)

where amplitude of the pole is

$$D(\ell) = D_0 [1 - \text{Re} S_\ell(BG)] \quad (7)$$

and the width of the pole is

$$\Gamma(\ell) = \Gamma_0 [1 - \text{Re} S_\ell(BG)] \quad (8)$$

The phase of the pole is represented by ϕ_{ℓ_0} . [1-4]

The seven parameters inputs r_0 , d , μ_M , D_0 , Γ_0 , ℓ_0 and ϕ_{ℓ_0} , respectively, used to get the smallest value of χ^2

One of the aims of this work is to investigate the change in total cross section of scattered ions when size of target ion change, for incident projectile. This study is also objected to better understanding of the diffractive features of elastic scattering of heavy ions and extract important parameters (like radius of interaction region of scattered ions R and diffusivity d.(3)

RESULT AND DISCUSSION

The available experimental data of scattering ^4He by different target nuclei ^{70}Ge , ^{72}Ge , ^{74}Ge and ^{76}Ge are analyzed using the combined model of McIntyre and Regge by fitting the calculated results to the experimental data. We use FORTRAN code to obtain the best fit of experiment data of angular distribution and the final choice of extracted parameters depend on the value of χ^2 for each model is. The χ^2 is defined by the expression:

$$\chi^2 = \frac{1}{N} \left(\sum_i^N [(\sigma_{\text{theory}}^i - \sigma_{\text{exp}}^i) / (\Delta\sigma_{\text{exp}}^i)]^2 \right)$$

Here σ_{theory}^i , σ_{exp}^i and $\Delta\sigma_{\text{exp}}^i$ are theoretical, experimental cross section and the corresponding error in cross section, respectively, N is the number of experimental data points. However, the average value of 10% of the experimental measurement is taken for each experimental error of the energy of the elastic scattering under study (1,4).

Elastic scattering of $^4\text{He} + ^{70,72,74,76}\text{Ge}$ target nuclei.

McIntyre plus Regge pole are used to analyze the experimental data of angular distribution for elastic scattering of α particle by different target nuclei ^{70}Ge , ^{72}Ge , ^{74}Ge and ^{76}Ge at Energy 25MeV

Figures 1 present the theoretical results of angular distribution for the elastic scatterings $^4\text{He} + ^{70,72,74,76}\text{Ge}$ at laboratory energy 25MeV, The experimental data (symbols) of angular distribution of elastic scattering of α particles by the target nucleus $^{70,72,74,76}\text{Ge}$ at laboratory energies 25MeV, compared to the theoretical results obtained using the combined model of McIntyre plus Regge (solid line) are shown.

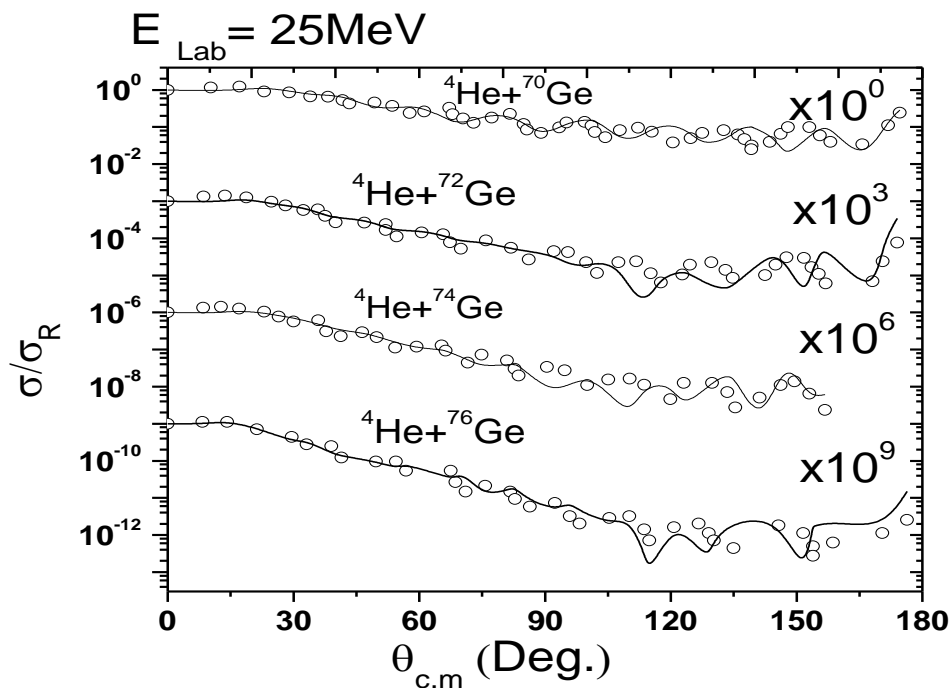


Figure 1: The experimental data (symbols) of angular distribution of elastic scattering of α particles by the target nucleus $^{70,72,74,76}\text{Ge}$ at laboratory energies 25MeV, are shown and compared to the theoretical results obtained using the combined model of McIntyre plus Regge (solid line).

The list of fitting parameters which also includes the values of χ^2 and other physical quantities for the elastic scatterings $4\text{He}+76\text{Ge}$, $4\text{He}+74\text{Ge}$, $4\text{He}+72\text{Ge}$ and $4\text{He} + 70\text{Ge}$ at fixed energy is shown in Tables 1.

Table 1. List of parameters for elastic scattering of α particles by the target nucleus $^{70,72,74,76}\text{Ge}$ at laboratory energies 25MeV, which are extracted from the analyses using McIntyre plus Regge pole model. The total reaction cross-sections $\sigma_r(\text{FM})$ and $\sigma_r(\text{GFM})$ are obtained from FM and GFM, respectively.

Elastic scattering	$4\text{He} + 76\text{Ge}$	$4\text{He} + 74\text{Ge}$	$4\text{He} + 72\text{Ge}$	$4\text{He} + 70\text{Ge}$
$E_{\text{Lab.}}$ (MeV)	25	25	25	25
r_o (fm)	1.55	1.30	1.25	1.125
μ (Rad)	0.38	0.29	0.22	0.27
d (fm)	0.34	0.325	0.23	0.155
ℓ_o	0.50	5.50	6	3.5
ϕ_{ℓ_o} (Deg.)	1	10	2.5	6
D_o	1	1	2	4
Γ_o	5	10	4.2	6
ℓ_g	14	10	9	8
Δ	7.30×10^{-1}	7.19×10^{-1}	5.13×10^{-1}	3.50×10^{-1}
R (fm)	9.025	7.252	7.18	6.42
d/R	3.76×10^{-2}	4.32×10^{-2}	3.20×10^{-2}	2.41×10^{-2}
p	8.147	8.22	8.23	8.22
n	4.03	4.03	4.03	4.03
h	10.21	12.25	12.82	14
θ_R (Rad)	5.6×10^{-1}	7.66×10^{-1}	7.66×10^{-1}	9.33×10^{-1}
θ_{Nuc} (Rad)	-1.93×10^{-1}	-2.0×10^{-1}	-1.09×10^{-1}	-1.03×10^{-1}
σ_r (mb) [GFM]	160	83.8	69.7	45.5
σ_r (mb) [FM]	164	88.7	73.3	59.6
χ^2	0.014	0.012	0.033	0.025

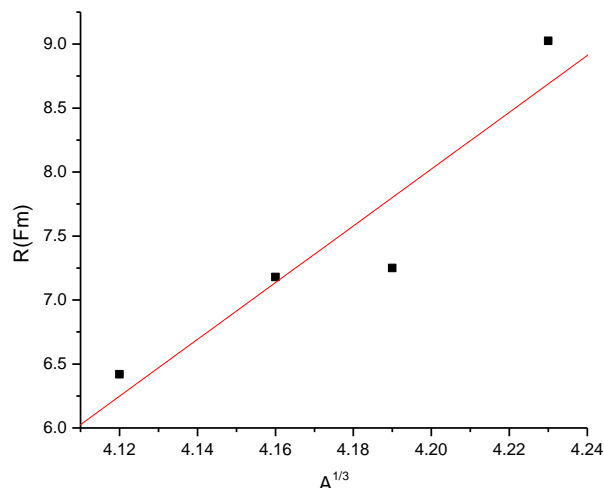


Figure 2. Interaction radius versus $A^{1/3}$ of different target nuclei at incident energy of 27MeV from analysis of McIntyre + regge pole model (symbols). The best least square fits for results obtained (solid line) is presented.

CONCLUSIONS

We have analyzed the elastic scattering α particle by different target nuclei 70Ge , 72Ge , 74Ge and 76Ge at Energy 25MeV within the framework of the parameterized model, There are two quantities determined type of diffraction pattern in the angular distribution; the diffraction parameter kR (which is equivalent to Δ or ℓ_g the angular momentum) and (the strength of the Coulomb interactions which represents by Sommerfeld parameter n). The Fresnel features in the angular distribution, which is determined by the parameter p , that the parameter p increases if the size of target nuclei increase, similar values of the parameters (n , h) or (ℓ_g , p) for oscillatory structure in elastic scatterings. , we using the parameters (r_o , d , μ , ℓ_o , ϕ_{ℓ_o} , D_o and Γ_o) in the combined model, The radius interaction region R is increasing when the atomic mass of target nucleus is increased the better formula of ($R = r_o A_T^{1/3} + r_\alpha$), The diffusivity parameter d has an effect on the slope of the oscillation and its increase with increase the target size, The increase in nuclear phase shift parameter μ cause to change the diffraction structure for the angular distributions calculated, the parameters (ℓ_o , ϕ_{ℓ_o} , D_o and Γ_o) used in backward angle, ℓ_o the orbital angular momentum which estimate the location for the pole, the D_o Amplitude and the Γ_o width exhibit the similar behavior the width of the pole, ϕ_{ℓ_o} which represent the phase angle determined the size of oscillation, the parameters (ℓ_o , ϕ_{ℓ_o} , D_o and Γ_o) are found vulnerable in the fitting process but accountable for reproducing the oscillatory structure of the experimental data. The quality of fittings using the adopted models is as good as that using the standard model.

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