

## Discharge Generation Quantum Effect on Storm Cloud Near Field Electrodynamic Model

**Omar Rodríguez Pinilla<sup>1</sup>, Jorge E López C<sup>1</sup>, Mikel F Hurtado M<sup>1\*</sup>**  
*Electronic Engineering Department, Universidad Central, Bogotá – Colombia.*

### Abstract

In the following work, a theoretical proposal is presented on the mechanism of electric discharge generation in a storm cloud under anisotropic medium (gas) conditions using the quantum model of near field electrostatics through paths integrals. The aim is calculate the quantum factor of possible trajectories fluctuation in a beam of charge carriers that follow in the cloud.

**Keywords:** Discharge, charge trajectory, charge carrier, storm

### THEORETICAL MODEL

Taking into account the near field electrodynamic model [1, 2, 3, 4], the possible trajectories that a certain particle can choses (in this case a charge carrier), depends on the conditions imposed by the environment, it is isotropic or not, and how much electromagnetic permissive it is. Just in the moment when the discharge begin on the storm cloud [5, 6, 7, 8], the propagation medium of charge carriers beam becomes very electromagnetic unstable and locally conductive.

In this theoretical development, the fluctuation factor is calculated taking into account the possible flux charge carrier's trajectories, which at the same time are the atmospheric discharge generators. We propose; using the near field perturbations model [8, 9, 10, 11], demonstrate how the first discharge is generated, in the very first moment of time and an elemental volume with N particles.

Using the theoretical model proposed by Feynman [12, 13], the quantum behavior of possible trajectories that could chose a certain charge carrier between a point Xb and Xa in a electromagnetic field configuration, is expressed as:

$$\langle x_b; t_b | x_a; t_a \rangle = \langle x_b | \widehat{H}(t) | x_a \rangle = \int dx_1 \dots \dots \int dx_j \langle x_b | e^{-i\frac{H}{\hbar}t} | x_{j+1} \rangle \langle x_{j+1} | x_j \rangle \langle x_j | x_a \rangle \quad (1)$$

Where the electromagnetic interaction Hamiltonian operator is:

$$\widehat{H} = \left[ \frac{1}{2m} \left( \hat{p} - \frac{e}{c} \hat{A} \right)^2 - \frac{k_e}{r^3} \hat{p}_0^2 + eV(r) - \mu B \right] \quad (2)$$

being:  $\hat{p}$  – momentum operator;  $\hat{A}$  – magnetic potential;  $\hat{p}_0$  – dipole moment;  $\mu$  – magnetic moment;  $B$  – magnetic field;  $V(r)$  – electric potential;  $k_e$  – dielectric constant; and  $m$  – electron mass.

The matrix electron that distinguishes the moment operator action over the propagation beam function is defined as [14, 15, 16]:

$$\langle x_{j+1} | p_j A_j | x_j \rangle = e^{-\frac{i}{\hbar} \tau U^*} \frac{A_j}{\hbar} \int p_j dp_j e^{-\frac{i}{\hbar} p_j^2 \frac{\tau}{2m} + \frac{i}{\hbar m c} p_j A_j \tau} \quad (3)$$

And the energy system (gas - charge carrier) could be expressed as:

$$U^* = \frac{1}{2m} \left( \frac{e}{c} A_j \right)^2 + eE x_j - \mu B \quad (4)$$

Then, the trajectory integral for the carrier is:

$$\begin{aligned} \langle x_b; t_b | x_a; t_a \rangle &= \langle x_b | \widehat{H}(t) | x_a \rangle \\ &= \int dx_1 \dots \dots \int dx_j \langle x_{j+1} | p_j A_j | x_j \rangle \langle x_{j+1} | x_j \rangle \langle x_j | x_a \rangle \\ &= \int dx_1 \dots \dots \int dx_j e^{-\frac{i}{\hbar} \tau U^*} \frac{A_j}{\hbar} \int p_j dp_j e^{-\frac{i}{\hbar} p_j^2 \frac{\tau}{2m} + \frac{i}{\hbar m c} p_j A_j \tau} \langle x_{j+1} | x_j \rangle \langle x_j | x_a \rangle \end{aligned} \quad (5)$$

And using the results of position integrals, the equation (5) lets calculate the fluctuation quantum factor of the possible beam trajectories or generated discharge on a storm cloud as:

$$\langle x_b; t_b | x_a; t_a \rangle = \sqrt{\frac{2\pi m}{i\tau \hbar}} \exp\left(\frac{i}{\hbar} U(x_j) \tau\right) \left(\frac{e}{2c} B_j\right) \sqrt{\frac{\pi}{a}} \left(\frac{b}{2a}\right) \exp\left(\frac{b^2}{4a}\right) \quad (6)$$

Where is obtained the fluctuation quantum factor to the trajectories for a charge carrier beam, given the expression:

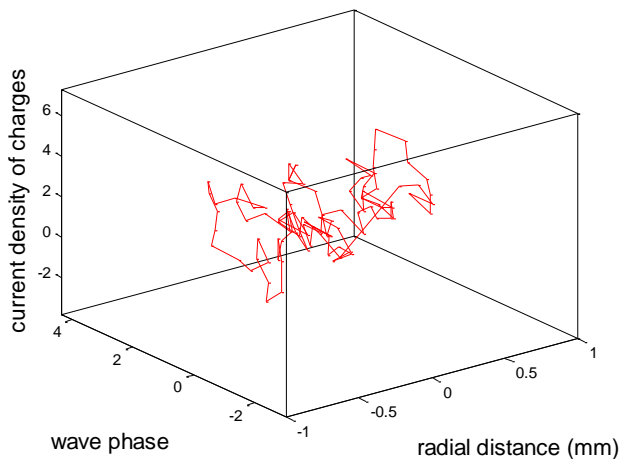
$$F_j = \sqrt{\frac{2\pi m}{i\tau \hbar}} \left(\frac{e}{2c} B_j\right) \sqrt{\frac{\pi}{a}} \left(\frac{b}{2a}\right) \exp\left(\frac{b^2}{4a}\right) \quad (7)$$

Taking into account that the coefficients for equation (7) are:

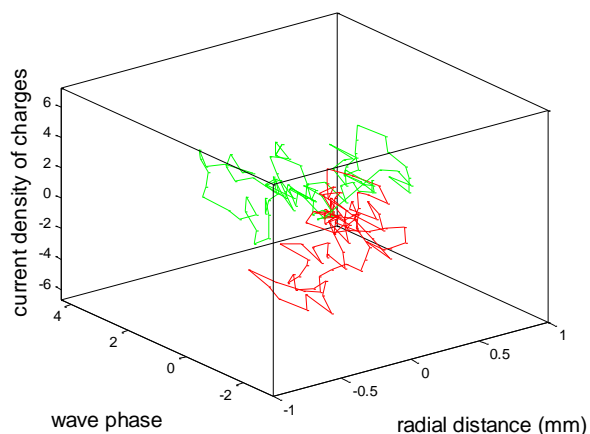
$$\begin{aligned} U_0 &= \frac{1}{\hbar} eV\tau = i1,518E15V\tau; \quad a = -\frac{i}{\hbar} \frac{1}{m} \left(\frac{e}{c} B_j\right)^2 \tau; \\ b &= -\frac{i}{\hbar} eE_j\tau; \quad d = \frac{i}{\hbar} U(x_j) \tau = \frac{i}{\hbar} eV\tau; \end{aligned} \quad (8)$$

### SIMULATED MODEL

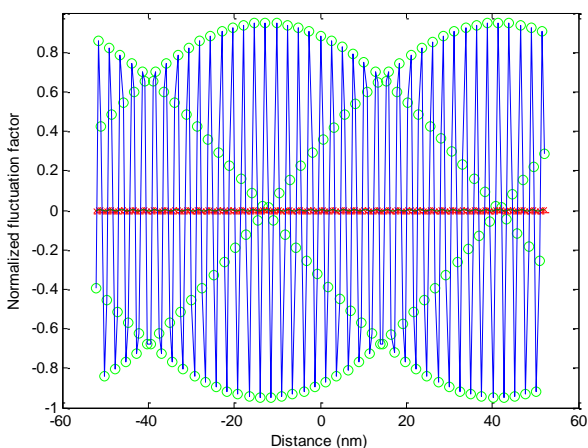
The first steps in the presented work were found and simulate one of the possible trajectories of a charge carrier on the cloud and later find the behavior of the fluctuation quantum factor of a group of trajectories. The figure 1, shows the possible trajectory simulation for a charge carrier on a storm cloud in anisotropic space conditions.



**Figure 1.** Simulated model of a possible trajectory for a charge carrier on a storm cloud in an anisotropy space



**Figure 2.** shows the simulated model using equation (7), which represents the normalized fluctuation factor for trajectory series of the charge carriers flux in unstable space conditions that means in the model of energy perturbations.



**Figure 3.** Simulated model that represents the normalized fluctuation factor for trajectory series of the charge carriers flux in unstable space conditions

## DISCUSSION AND CONCLUSIONS

- The showed theoretical proposal will give an experimental model that validate the results and have a mechanism that specify the behavior of the discharged cloud phenomena in order to understand completely the atmosphere beam behavior.
- Although each possible trajectory described by the load flow in the storm cloud, in the perturbation model proposed in the present work, is homotopically equivalent, the discharge conditions mean that at each point of the same the trajectory due to the number of vacancies and become multiply connected, which makes their paths diverse after a time  $t$ . The previous statement can be seen in Figure 3, in which two possible trajectories were compared in the discharge, finding similarity conditions and in turn their high divergence at the time of generating their final trajectories.

## ACKNOWLEDGEMENT

We want to thank to Electronic Engineering Department, MAXWELL Research Group and Solid State Micro and Nanosystems staff Universidad Central.

## REFERENCES

- [1] Sakurai j. J. Modern Quantum Mechanics. Addison Wesley. 1994
- [2] ND Mermin, Thermal properties of the inhomogeneous electron gas, Phys. Rev. 137 A1441-1443 (1965).
- [3] Devendraa Siingh. Et al. Journal of Atmospheric and Solar-Terrestrial Physics. Volume 134, November 2015, Pages 78-10.
- [4] Victor F. Tarasenko. Et al. Review of supershort avalanche electron beam during nanosecond-pulse discharges in some gases. Matter and Radiation at Extremes 2 (2017) 105e116.
- [5] J.D. Bulnes. Propagadores cuánticos calculados de acuerdo con el postulado de Feynman con caminos aproximados por polinomios. Revista mexicana de física e 55 (1) 34–43. (2009).
- [6] Rodríguez P. Omar. Uv radiation by the Debye sphere interaction plasma – metal nanoparticles on the surface of plant tissue. International Journal of Applied Engineering Research and Development (IJAERD) ISSN(P): 2250-1584; ISSN(E): 2278-9383. Vol. 7, Issue 3, Jun 2017, 11-16.
- [7] B J Berne, and D Thirumalai. On the Simulation of Quantum Systems: Path Integral Methods. Annual Review of Physical Chemistry. Vol. 37: 401-424 (Volume publication data October 1986).

- [8] T.Czech, A.T.Sobczyk, A.Jaworek, et al. Journal of Electrostatics. Volume 70, Issue 3, June 2012, Pages 269-284.
- [9] Earle R. Williams. Electricity in the Atmosphere: Global Electrical Circuit. Encyclopedia of Atmospheric Sciences (Second Edition), 2015.
- [10] Fabio Nicola. Convergence in  $L^p$  for Feynman path integrals. Advances in Mathematics. Volume 294, 14 May 2016, Pages 384-409.
- [11] S. Albeverio and S. Mazzucchi. The time-dependent quartic oscillator—a Feynman path integral approach. Journal of Functional Analysis 238 (2006) 471–488.
- [12] Naoto Kumano-go. Phase space Feynman path integrals with smooth functional derivatives by time slicing approximation. Bull. Sci. math. 135 (2011) 936–987.
- [13] Preben Hvelplund. Et al. Experimental studies of the formation of cluster ions formed by corona discharge in an atmosphere containing  $\text{SO}_2$ ,  $\text{NH}_3$ , and  $\text{H}_2\text{O}$ . International Journal of Mass Spectrometry. Volumes 341–342, 1 May 2013, Pages 1-6.
- [14] V. V. Surkov V. and M. Hayakawa. Underlying mechanisms of transient luminous events. Ann. Geophys., 30, 1185–1212, 2012.
- [15] L. P. Babich, E. I. Bochkov, and I. M. Kutsyk. Mechanism of Generation of Runaway Electrons in a Lightning Leader. *ISSN 0021\_3640, JETP Letters, 2014, Vol. 99, No. 7, pp. 386–390. © Pleiades Publishing, Ltd., 2014.*
- [16] L. P. Babich. E. I. Bochkov. Et Al. Analyses of electron runaway in front of the negative streamer channel. Journal of Geophysical Research: Space Physics. 10.1002/2017JA023917.