

Efficient Compensation of Receiver IQ Imbalance in OFDM System

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ABSTRACT

Transceivers based on a direct conversion architecture introduces an unwanted limited image rejection and degrades the accuracy of carrier estimation due to presence of I/Q imbalance. In this paper, we proposed an efficient scheme to compensate IQ imbalance in OFDM receivers. Simulation results confirmed that the proposed scheme performance is very close to the ideal case.

Keywords- IQ imbalance, OFDM, Receiver, AWGN

1. Introduction

OFDM is a widely recognized and standardized modulation technique [1], [2]. Due to lower complexity and higher flexibility, direct conversion receivers are preferred to super heterodyne transceivers in OFDM systems. Unfortunately, OFDM transceivers are sensitive to non-idealities in the receiver front-end [3]. IQ imbalance has been identified as a key front-end effect for OFDM systems. In practice, due to manufacturing imperfections, there would be phase and amplitude mismatch in the phase (I) and quadrature (Q) branches of the IQ-receiver commonly known as IQ-imbalance [3]. The compensation of IQ-imbalance in MIMO-OFDM has gained a lot of attention recently [4], [5]. Phase noise is another major impairment caused by non-ideal oscillator which introduces random phase fluctuations at the oscillator output resulting in distortion of the signals [3]. The effect of phase noise is more severe in OFDM systems and is studied extensively in the literature [6], [7]. These works state that the effect of phase noise can be broken down into common phase error (CPE) and inter-carrier interference (ICI) with CPE is more prominent for systems with less phase noise. Analysis of performance and compensation techniques are proposed for OFDM and MIMO-OFDM systems in the literature and can be found in [7] -[9].

Joint IQ-imbalance and phase noise compensation techniques for single-input-single-output (SISO) systems have been previously discussed in [10] and [11]. However, joint treatment of these impairments for MIMO-OFDM systems have not been studied extensively. In [12], joint estimation and compensation scheme for MIMO-OFDM systems, assuming quasi-static channel is proposed. The authors first develop a compensation scheme for SISO systems and generalize it to the MIMO case. The proposed method requires more training symbols with increasing number of transmit-receive antennas and the complexity of the scheme is high due to the required maximum likelihood (ML) estimation. In this paper, we proposed an efficient scheme to compensate IQ imbalance in OFDM receivers and compared its performance with existing IQ imbalance compensation schemes. The paper is organized as follows, in section 2 system model is described. In section 2.1 proposed schemes for IQ imbalance compensation is explained. In section 3 simulation results are presented and in section 4 the paper is concluded.

2. System Model

At the transmitter serial data stream is converted to parallel data using serial to parallel converter, modulated and passed through N-point FFT block and cyclic prefix are added before transmitting the signal. Let $s_{n,k}$ be the k^{th} frequency domain OFDM symbol to be transmitted from the n^{th} transmit antenna whose time domain representation is given by $\overline{s_{n,k}} = F^{-1}(s_{n,k})$ where F^{-1} is the inverse Fourier transform operation. The vector that contains all the $N + N_{\text{cp}} + L - 1$ discrete time domain received signal samples at the m^{th} receive antenna is then given by

$$\overline{r_{m,k}} = \sum_{n=1}^M h_{m,n} * \overline{s_{n,k}} + w_m$$

Where $h_{m,n}$ the channel impulse response of the multipath channel from the n^{th} transmit to the m^{th} receive antenna for the k^{th} OFDM symbol. $\overline{s_{n,k}}$ is the transmitted discrete time signal vector from the n^{th} antenna to m^{th} antenna. w_q is the added additive white Gaussian noise (AWGN) at the m^{th} receive antenna. At the receiver the cyclic prefix of the received signal is removed, the signal samples are then converted into parallel streams and fed into FFT block with size N. The equivalent frequency domain received signal model at the i^{th} subcarrier

$$r_k(i) = H_k(i)s_k(i) + \eta_k(i)$$

Where $r_k(i)$ is the received signal, $H_k(i)$ is the frequency response of the channel, $s_k(i)$ is the transmitted signal at i^{th} sub carrier of k^{th} OFDM symbol.

2.1 IQ Imbalance Model

The time domain oscillator output with frequency independent IQ imbalance can be given as [23],[24]

$$y(t) = \cos(\omega_c t) + j\varepsilon \sin(\omega_c t + \phi)$$

Where ε and ϕ are amplitude and in-phase mismatches respectively. $Y(t)$ can also be given as

$$\begin{aligned} y(t) &= (1 + \varepsilon) \cos \Delta\phi \Re\{x\} \\ &- j(1 - \varepsilon) \sin \Delta\phi \Re\{x\} \\ &+ j(1 - \varepsilon) \cos \Delta\phi \Im\{x\} \\ &- (1 + \varepsilon) \sin \Delta\phi \Im\{x\} \end{aligned}$$

$$y(t) = (\cos \Delta\phi - j\varepsilon \sin \Delta\phi).x - (\varepsilon \cos \Delta\phi - j \sin \Delta\phi).x^*$$

$$y(t) = \alpha.x + \beta.x^* \quad (1)$$

Where $y(t)$ represents signal with imbalance, $\Re\{x\}$ represents real part of signal and $\Im\{x\}$ represents imaginary part of signal.

$$\alpha = \cos \Delta\phi + j\varepsilon \sin \Delta\phi$$

$$\beta = \varepsilon \cos \Delta\phi - j \sin \Delta\phi$$

If no IQ imbalance is present, then $\alpha = 1$ and $\beta = 0$ and then (1) reduces to $y = x$.

We analyze the effect of the IQ imbalance on OFDM transmission. We consider AWGN channel. If x is the transmitted OFDM symbol (in the frequency domain), then $IFFT(x)$ is the incoming time domain signal in the receiver. Applying the IQ imbalance (1) and taking the FFT leads to

$$R = FFT\{\alpha \times IFFT(x) + \beta \times IFFT(x)^*\}$$

$$R = \alpha \times x + \beta \times x^*$$

2.2 Cost function for IQ imbalance

$Y(t)$ is the received signal at the OFDM receiver, equation (1) can also be given as

$$y(t) = A \cos(\omega_c t) + j\alpha A \sin(\omega_c t + \phi + \varepsilon)$$

Where α amplitude is mismatch and ε is in-phase mismatch

At the OFDM receiver the received signal with IQ imbalance can be given as

$$R(m) = \left(\frac{1}{N} \times \alpha \times \sum_{k=-N/2}^{N/2-1} X(k) e^{j2\pi mk/2N} \right) + \left(\frac{1}{N} \times \beta \times \sum_{k=-N/2}^{N/2-1} X^*(k) e^{j2\pi mk/2N} \right) \quad (2)$$

where $X(k)$ denote the frequency domain, transmitted data for the k -th subcarrier, N is the number of subcarriers. Equation (2) can be written as

$$R(m) = \left(\frac{1}{N} \times (\cos \Delta\phi + j\varepsilon \sin \Delta\phi) \times \sum_{k=-N/2}^{N/2-1} X(k) e^{j2\pi mk/2N} \right) + \left(\frac{1}{N} \times (\varepsilon \cos \Delta\phi - j \sin \Delta\phi) \times \sum_{k=-N/2}^{N/2-1} X^*(k) e^{j2\pi mk/2N} \right)$$

$$R(m) = \left(\frac{1}{N} \times \left(\frac{e^{\Delta\phi} + e^{-\Delta\phi}}{2} + j\varepsilon \frac{e^{\Delta\phi} - e^{-\Delta\phi}}{2j} \right) \times \sum_{k=-N/2}^{N/2-1} X(k) e^{j2\pi mk/2N} \right) + \left(\frac{1}{N} \times \left(\varepsilon \frac{e^{\Delta\phi} + e^{-\Delta\phi}}{2} - j \frac{e^{\Delta\phi} - e^{-\Delta\phi}}{2j} \right) \times \sum_{k=-N/2}^{N/2-1} X^*(k) e^{j2\pi mk/2N} \right)$$

$$R(m) = \left(\frac{1}{N} \times \frac{((1+\varepsilon)e^{\Delta\phi} + (1-\varepsilon)e^{-\Delta\phi})}{2} \times \sum_{k=-N/2}^{N/2-1} X(k) e^{j2\pi mk/2N} \right) + \left(\frac{1}{N} \times \frac{((\varepsilon-1)e^{\Delta\phi} + (\varepsilon+1)e^{-\Delta\phi})}{2} \times \sum_{k=-N/2}^{N/2-1} X^*(k) e^{j2\pi mk/2N} \right)$$

$$R(m) = \left(\frac{1}{N} \times \frac{((1+\varepsilon)e^{\Delta\phi} + (1-\varepsilon)e^{-\Delta\phi})}{2} \times \sum_{k=-N/2}^{N/2-1} X(k) e^{j2\pi mk/2N} \right) + \left(\frac{1}{N} \times \frac{((\varepsilon-1)e^{\Delta\phi} + (\varepsilon+1)e^{-\Delta\phi})}{2} \times \sum_{k=-N/2}^{N/2-1} X^*(k) e^{j2\pi mk/2N} \right) \quad (3)$$

Equation (3) can be rearranged as

$$\begin{aligned}
R(m) &= \left(\frac{1+\varepsilon}{2N} \times \sum_{k=-N/2}^{N/2-1} X(k) e^{j2\pi nk/2N} e^{\Delta\phi} \right. \\
&+ \frac{(1-\varepsilon)}{2N} \times \sum_{k=-N/2}^{N/2-1} X(k) e^{j2\pi nk/2N} e^{-\Delta\phi} \\
&+ \frac{(\varepsilon-1)}{2N} \times \sum_{k=-N/2}^{N/2-1} X^*(k) e^{j2\pi nk/2N} e^{\Delta\phi} \\
&\left. + \frac{(\varepsilon+1)}{2N} \times \sum_{k=-N/2}^{N/2-1} X^*(k) e^{j2\pi nk/2N} e^{-\Delta\phi} \right)
\end{aligned}$$

$$\begin{aligned}
R(m) &= \left(\frac{(1+\varepsilon)}{2N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi nk/2N} e^{\Delta\phi} \right. \\
&+ \frac{(1+\varepsilon)}{2N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi nk/2N} e^{\Delta\phi} + \\
&\frac{(1-\varepsilon)}{2N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi nk/2N} e^{-\Delta\phi} \\
&+ \frac{(1-\varepsilon)}{2N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi nk/2N} e^{-\Delta\phi} \\
&+ \frac{(\varepsilon-1)}{2N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi nk/2N} e^{\Delta\phi} \\
&- \frac{(\varepsilon-1)}{2N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi nk/2N} e^{\Delta\phi} \\
&+ \frac{(\varepsilon+1)}{2N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi nk/2N} e^{-\Delta\phi} \\
&\left. - \frac{(\varepsilon+1)}{2N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi nk/2N} e^{-\Delta\phi} \right)
\end{aligned}$$

$$\begin{aligned}
R(m) &= \left(\frac{\varepsilon}{N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi nk/2N} e^{\Delta\phi} \right. \\
&+ \frac{1}{N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi nk/2N} e^{\Delta\phi} \\
&+ \frac{1}{N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi nk/2N} e^{-\Delta\phi} \\
&\left. - \frac{\varepsilon}{N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi nk/2N} e^{-\Delta\phi} \right)
\end{aligned}$$

$$\begin{aligned}
R(m) &= \left(\frac{\varepsilon}{N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi mk/2N} e^{\Delta\phi}\right) \\
&+ \frac{1}{N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi mk/2N} e^{-\Delta\phi} \\
&- \frac{\varepsilon}{N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi mk/2N} e^{-\Delta\phi} \\
&+ \frac{1}{N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi mk/2N} e^{\Delta\phi}
\end{aligned}$$

Let

$$\begin{aligned}
R_a(m) &= \frac{1}{N} (\text{abs}(\varepsilon \times \text{IFFT}(\Re(x(k))) \times e^{\Delta\phi}) \\
&+ \text{IFFT}(\Re(x(k))) \times e^{-\Delta\phi}) \\
&+ \text{abs}(-\varepsilon \times \text{IFFT}(\Im(x(k))) \times e^{-\Delta\phi}) \\
&+ \text{IFFT}(\Im(x(k))) \times e^{\Delta\phi})
\end{aligned}$$

Where abs refers to absolute value.

$$\begin{aligned}
R_a(m) &= \left(\frac{\varepsilon}{N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi mk/2N} e^{\Delta\phi}\right) \\
&+ \frac{1}{N} \times \sum_{k=-N/2}^{N/2-1} \Re(X(k)) e^{j2\pi mk/2N} e^{-\Delta\phi} \\
&+ \frac{\varepsilon}{N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi mk/2N} e^{-\Delta\phi} \\
&+ \frac{1}{N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi mk/2N} e^{\Delta\phi}
\end{aligned}$$

Then $R_y(m) = R(m) - R_a(m)$ will result

$$R_y(m) = (R(m) - R_a(m)) = -\frac{2\varepsilon}{N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi mk/2N} e^{-\Delta\phi}$$

At the receiver let us consider time shift version of $R_y(m)$ i.e. $R(m-t)$

$$R_y(m-t) = -\frac{2\varepsilon}{N} \times \sum_{k=-N/2}^{N/2-1} \Im(X(k)) e^{j2\pi(m-t)k/2N} e^{-\Delta\phi}$$

If in-phase mismatch doesn't exist i.e. $\phi = 0$

$$\text{Then } FFT(R_y(m)) = FFT(R_y(m-t)) \times e^{j2\pi k / 2N} \quad (4)$$

If in-phase mismatch exists and $\phi \neq 0$, then time shift invariant property of DFT does not hold any more and

$$FFT(R_y(m)) \neq FFT(R_y(m-t)) \times e^{j2\pi k / 2N}$$

Thus, the in-phase mismatch should be compensated exactly before operation FFT on $R(m)$ and $R(m-t)$. we introduce a trial in-phase mismatch estimation value $\hat{\phi}$ and compensate the effects of in-phase mismatch in $R_y(m)$ and $R_y(m-t)$, by forming the compensated signals $R_y(m)e^{-\Delta\phi}$ and $R_y(m-t)e^{j2\pi k / 2N} e^{-\Delta\phi}$. In the frequency domain, the compensated signals can be expressed as follows:

$$r_y(l, \hat{\phi}) = \sum_{m=0}^{N-1} \{R_y(m)e^{-\Delta\phi}\} e^{-j2\pi ml / N}$$

$$r_{iy}(l, \hat{\phi}) = \sum_{m=0}^{N-1} \{R_y(m-t)e^{-\Delta\phi} e^{j2\pi k / 2N}\} e^{-j2\pi ml / N}$$

As given in equation (4) if there is no in-phase mismatch i.e. $\phi = \hat{\phi}$, then $r_y(l, \hat{\phi}) - r_{iy}(l, \hat{\phi}) = 0$, if in-phase mismatch exists i.e. $\phi \neq \hat{\phi}$ then $r_y(l, \hat{\phi}) - r_{iy}(l, \hat{\phi}) \neq 0$, using $r_y(l, \hat{\phi})$ & $r_{iy}(l, \hat{\phi})e^{j2\pi ml / N}$ we define least squares cost function

$$\zeta(\hat{\phi}) = \sum_{m=0}^{N-1} |r_y(l, \hat{\phi}) - r_{iy}(l, \hat{\phi})e^{j2\pi ml / N}|^2$$

Therefore in-phase mismatch is estimated and compensated searching for $\hat{\phi}$ that minimizes the value of cost function given in equation (5). Thus, the in-phase mismatch estimate is given as

$$\hat{\phi} = \arg \min_{\hat{\phi}} \zeta(\hat{\phi}) = \arg \min_{\hat{\phi}} \sum_{m=0}^{N-1} |r_y(l, \hat{\phi}) - r_{iy}(l, \hat{\phi})e^{j2\pi ml / N}|^2 \quad (5)$$

If quadrature-phase mismatch (ε)=0 then $\alpha = \Re(\alpha)$, if quadrature-phase mismatch exists i.e. (ε) $\neq 0$ then $\alpha \neq \Re(\alpha)$ using the relation, we define least squares cost function

$$\xi(\hat{\varepsilon}) = |\alpha - \Re(\alpha)|^2$$

Therefore quadrature-phase mismatch is estimated and compensated searching for $\hat{\varepsilon}$ that minimizes the value of cost function given in equation (6). Thus, the quadrature-phase mismatch estimate is given as

$$\hat{\varepsilon} = \arg \min_{\hat{\varepsilon}} \xi(\hat{\varepsilon}) = \arg \min_{\hat{\varepsilon}} |\alpha - \Re(\alpha)|^2 \quad - \quad (6)$$

3. Simulation Results

A typical OFDM system is simulated to evaluate the performance of the compensation scheme for receiver I/Q imbalance in AWGN channel. The performance comparison is made with an ideal system with no front-end distortion and with a system with no compensation algorithm included. The parameters employed in the simulation are as follows: OFDM symbol length of $N=64$, cyclic prefix of $CP=16$. The step size of the adaptive equalizer is kept at 0.2.

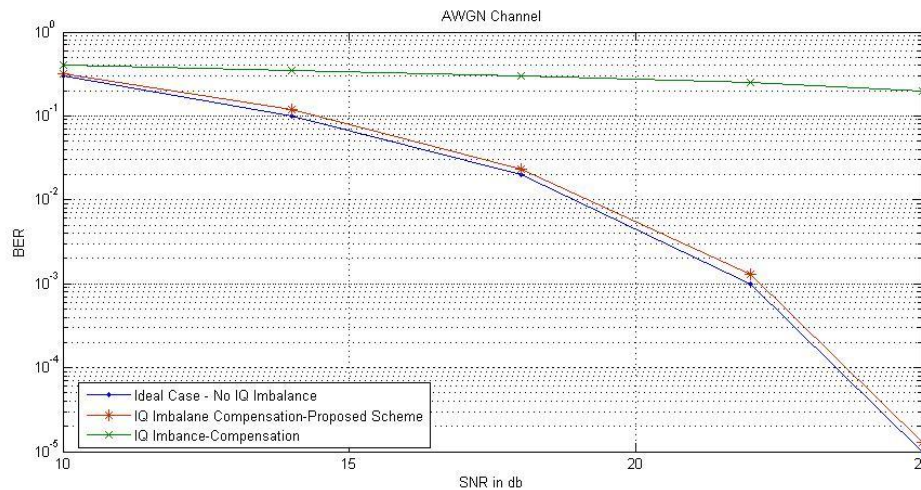


Figure 1 BER Vs SNR comparison for OFDM system with no IQ imbalance, IQ imbalance with compensation using proposed scheme and without compensation in AWGN channel (non fading).

We consider IQ amplitude imbalance of $\varepsilon = 5\%$ and phase imbalance of $\phi = 5^\circ$, at the receiver. Fig.1 shows the performance curves obtained for BER versus SNR for an uncoded 64QAM OFDM system. With no compensation scheme in place, the OFDM system is unusable. Even for the case when there is only transmitter and receiver IQ imbalance and no CFO, the BER is very high. For the case with the proposed compensation scheme employed, the curves are very close to the ideal situation with no front-end distortion.

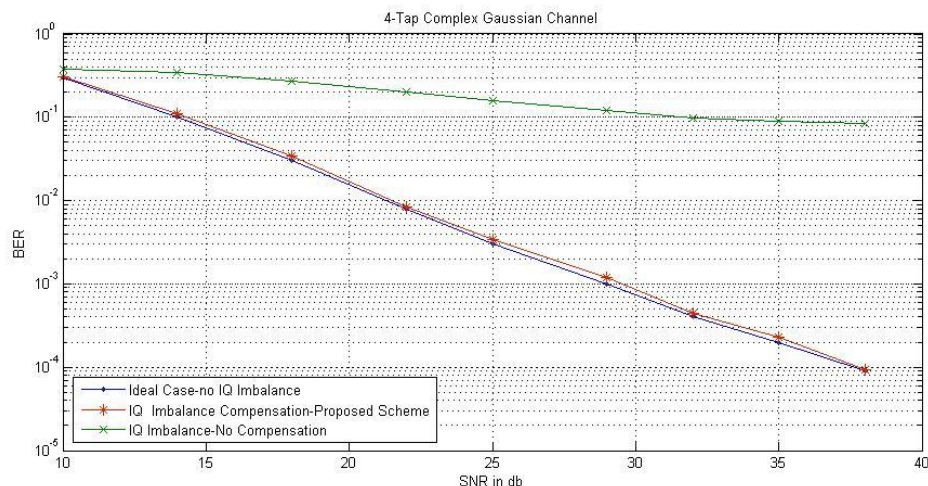


Figure 2 BER Vs SNR comparison for OFDM system with no IQ imbalance, IQ imbalance with compensation using proposed scheme and without compensation in 4-Tap Complex Gaussian channel (fading).

The compensation performance depends on how accurately the adaptive equalizer coefficients can converge to the ideal values. The design of zero-IF receivers typically yields an IQ imbalance on the order of [19]. The performance curves clearly demonstrate that for such IQ imbalance values compensation is necessary to enable a high data rate communication. Moreover, very large IQ imbalance values can be corrected just as easily. Thus, the presented IQ mitigation allows to greatly relax the zero-IF design specifications.

Conclusion

The I/Q imbalance in radio frequency (RF) impairments in direct conversion architecture based transceivers results in severe performance degradation. In this paper, we proposed an efficient scheme to compensate IQ imbalance in OFDM receivers. Simulation results confirmed that the proposed scheme performance is very near to ideal case (no IQ imbalance).

References

- [1] J. A. C. Bingham, "Multicarrier modulation for data transmission: an idea whose time has come," *IEEE Communications Magazine*, vol. 28, no. 5, pp. 5–14, 1990.
- [2] "IEEE standard 802.11a-1999: wireless LAN medium access control (MAC) & physical layer (PHY) specifications, highspeed physical layer in the 5 GHz band," 1999.

- [3] I. Koffman and V. Roman, "Broadband wireless access solutions based on OFDM access in IEEE 802.16," *IEEE Communications Magazine*, vol. 40, no. 4, pp. 96–103, 2002.
- [4] "ETSI Digital Video Broadcasting; Framing structure, Channel Coding & Modulation for Digital TV," 2004.
- [5] A. A. Abidi, "Direct-conversion radio transceivers for digital communications," *IEEE Journal of Solid-State Circuits*, vol. 30, no. 12, pp. 1399–1410, 1995.
- [6] C.-L. Liu, "Impacts of I/Q imbalance on QPSK-OFDM-QAM detection," *IEEE Transactions on Consumer Electronics*, vol. 44, no. 8, pp. 984–989, 1998.
- [7] S. Fouladifard and H. Shafiee, "Frequency offset estimation in OFDM systems in presence of IQ imbalance," in *Proceedings of the International Conference on Communications (ICC '03)*, pp. 2071–2075, Anchorage, Alaska, USA, May 2003.
- [8] J. Tubbax, B. Come, L. Van der Perre, M. Engels, M. Moonen, and H. D. Man, "Joint compensation of IQ imbalance and carrier frequency offset in OFDM systems," in *Proceedings of the Radio and Wireless Conference*, pp. 39–42, Boston, Mass, USA, August 2003.
- [9] F. Horlin, A. Bourdoux, and L. Van Der Perre, "Lowcomplexity EM-based joint acquisition of the carrier frequency offset and IQ imbalance," *IEEE Transactions on Wireless Communications*, vol. 7, no. 6, Article ID 4543073, pp. 2212–2220, 2008.
- [10] I. Barhumi and M. Moonen, "IQ-imbalance compensation for OFDM in the presence of IBI and carrier-frequency offset," *IEEE Transactions on Signal Processing*, vol. 55, no. 1, pp. 256–266, 2007.
- [11] A. Tarighat and A. H. Sayed, "Joint compensation of transmitter and receiver impairments in OFDM systems," *IEEE Transactions on Wireless Communications*, vol. 6, no. 1, pp. 240–247, 2007.
- [12] [D. Tandur and M. Moonen, "Joint adaptive compensation of transmitter and receiver IQ imbalance under carrier frequency offset in OFDM-based systems," *IEEE Transactions on Signal Processing*, vol. 55, no. 11, pp. 5246–5252, 2007.
- [13] K.Seshadri Sastry, Prasad Babu.M.S(2013), "Adaptive Population Sizing Genetic Algorithm Assisted Maximum Likelihood Detection of OFDM Symbols in the Presence of Nonlinear Distortions" *International Journal of Computer Network and Information Security*, June 2013, Volume 5, issue 7, pp 58-65, DOI: 10.5815/ijcnis.2013.07.07, , print ISSN 2074-9090, online ISSN 2074-9104, MECS publications, Hong Kong.
- [14] K.Seshadri Sastry," Adaptive Modulation Using Neuro-Fuzzy (N-F) Controller for OFDM System", Vol. 1, No. 2, pp. 85-89, June 2013. DOI: 10.12720/ijeee.1.2.85-89, 2013 4th International Conference on Signal and Information Processing, 06-07 July 2013, Kowloon, Hong Kong.
- [15] Prasad Babu .M.S, K. Seshadri Sastry , "Secant Method Based ML Estimation of Carrier Frequency Offset in OFDM System", *International Journal of*

- Computer Science and information Security, ISSN 1947-5500, April 2012, Volume 10(4), pp 125-128.
- [16] Ayesha Ijaz, Adegbenga B. Awoseyila and Barry G. Evans," IMPROVED SNR ESTIMATION FOR BPSK AND QPSK SIGNALS
- [17] K.Seshadri Sastry (2012), "Frequency Offset Estimation Based on Cyclostationary Statistics Induced by Cyclic Prefix" *International Journal of Electronics, Computer and Communications Technologies* , May 2012, Vol. 2(3), pp 6-8.
- [18] Lee, J., Lou, H.-L., Toumpakaris, I., & Cioffi, J. M. (2006). SNR analysis of OFDM systems in the presence of carrier frequency offset for fading channels. *IEEE Communication Letters*, 5, 12.
- [19] Jallon, P. (2008). An algorithm for detection of DVB-T signals based on their second order statistics. *EURASIP Journal on Wireless Communications and Networking*, 2008(article ID 538236).
- [20] K.Seshadri Sastry, Prasad Babu .M.S (2010), "Code Division Multiplexing Using AI Based Custom Constellation Scheme – Efficient Modulation for High Data Rate Transmission" *International Journal of Engineering Science and Technology (ISO Certified)*, ISSN: 0975-5462, June 2010, Volume 2 (6) , pp 2377-2383 .
- [21] K.Seshadri Sastry, Prasad Babu .M.S (2010), "Fuzzy Logic Based Adaptive Modulation Using Non Data Aided SNR Estimation for OFDM System" *International Journal of Engineering Science and Technology (ISO Certified)*, ISSN: 0975-5462, June 2010, Volume 2 (6), pp 2384-2392.
- [22] Wiesel, J. Goldberg, and H. Messer, "Non-data-aided signal-to noise- ratio estimation," in *Proc. IEEE Int. Conf. Commun.*, Apr. 2002, vol. 1, pp. 197–201.
- [23] S. M. Kay, *Fundamentals of Statistical Signal Processing—Detection Theory*. Englewood Cliffs, NJ: Prentice-Hall, 1998.
- [24] K.Seshadri Sastry, Prasad Babu .M.S (2010), "AI Based Digital Companding Scheme for OFDM System Using Custom Constellation Mapping and Selection" *International Journal on Computer Science and Engineering*, ISSN: 0975-3397, July 2010, Volume 2 (4), pp1381-1386.
- [25] Pollet, T., Bladel, M. V., & Moeneclaey, M. (1995). BER sensitivity of OFDM systems to carrier frequency offset and wiener phase noise. *IEEE Transactions on Communications*, 43(2/3/4), 191–193.
- [26] Lashkarian, N., & Kiaei, S. (2000). Class of cycle-based estimator for frequency offset estimation of OFDM systems. *IEEE Transactions on Communications*, 48(12), 2139–2149.
- [27] K.Seshadri Sastry, Prasad Babu .M.S (2010), "Custom Modulation Scheme for Enhanced Voice Quality in Software Defined Radio ", *IEEE ICSESS 2010*, Beijing , China, pp 376-379.
- [28] E. Nemer, R. Goubran and S. Mahmoud, "SNR Estimation of speech signals using subbands and fourth-Order statistics,"*IEEE Signal Processing Letters*, vol. 6, no. 7, pp. 171-174, Fig. 4 shows the average of the estimated SNRs obtained July 1999.

- [29] K.Seshadri Sastry, Prasad Babu .M.S (2010), “Adaptive Modulation for OFDM System Using Fuzzy Logic Interface”, July 18, 2010, IEEE ICSESS, PP 368-371.
- [30] K.Seshadri Sastry, Prasad Babu .M.S (2010), ” SNR Estimation for QAM Signals Using Fuzzy Logic Interface”, IEEE ICCSIT 2010, July 2010, pp 413-416
- [31] K. Balachandran, S. Kabada, and S. Nanda, “Rate adaptation over mobile radio channels using channel quality information,” in Proceedings of IEEE Global Telecommunications Conference, Globecom’98 Communication Theory Mini Conference Record, 1998, pp. 354-356.
- [32] K.Seshadri Sastry, Prasad Babu .M.S (2010),” AI Based Digital Companding Scheme for Software Defined Radio” IEEE ICSESS , 2010, pp 417- 419
- [33] K. Balachandran, S. R. Kadaba, and S. Nanda, “Channel quality estimation and rate adaption for cellular mobile radio,” IEEE J. Sel. Areas Commun., vol. 17, no. 7, pp. 1244–1256, Jul. 1999.
- [34] K.Seshadri Sastry, Prasad Babu .M.S (2010) ,”Digital Companding Scheme Using AI Based Custom Constellation Mapping and Selection”, IEEE ICSESS 2010 , Beijing , China, pp 364-367.
- [35] Xu, H., Wei, G., & Zhu, J. (2005). A novel SNR estimation algorithm for OFDM. In Proceedings of IEEE vehicular technology conference (Vol. 5, pp. 3068–3071).
- [36] Yi, W., Lihua, L., Ping, Z., Zemin, L., & Yu, Z. (2007). A new noise variance estimation algorithm for multiuser OFDM systems. In Proceedings of IEEE conference on personal, indoor and mobile radio communications (pp. 1–4)
- [37] K.Seshadri Sastry (2012) “Adaptive Modulation for OFDM System Using Fuzzy Logic Interface” in book named “Digital Communications”, published by Intech publications, Croatia, Europe, March 2012, pp 119-138.