

A Novel Wavelet-Based Fuzzy Based Fluorescence Image Denoising Approach With Optimized Variance-Stabilizing Transformations

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Abstract

Nowadays, Fluorescent protein microscopy imaging is one of the most important tools in biomedical research. However, the resulting images present a low signal to noise ratio and time intensity decay due to the photobleaching effect. This phenomenon is a consequence of the decreasing on the radiation emission efficiency of the tagging protein. This occurs because the fluorophore permanently loses its ability to fluoresce, due to photochemical reactions induced by the incident light. The Poisson multiplicative noise that corrupts these images, in addition with its quality degradation due to photobleaching, make long time biological observation processes very difficult. In proposed method a wavelet shrinkage algorithm based on fuzzy logic and the DT-DWT scheme with Anscombe transformation is used. In particular, intra-scale dependency within wavelet coefficients is modeled using a fuzzy feature. This model differentiates the important coefficients and the coefficients belong to image discontinuity and noisy coefficients. This fuzzy model is used to enhance the wavelet coefficients' information in the shrinkage step which uses the fuzzy membership function to shrink wavelet coefficients based on the fuzzy feature. This study examines image denoising algorithm in the dual-tree discrete wavelet transform, which is the new shiftable and modified version of discrete wavelet transform. Simulation result shows our approach achieves a substantial improvement in both PSNR and Visual quality.

Keywords: Mixed-Poisson-Gaussian, Poisson-Gaussian unbiased risk estimate, Fluorescence, Anscombe transformation, Image denoising, Dual-tree discrete wavelet transform, Fuzzy membership function.

1. INTRODUCTION

Fluorescence live-cell imaging is generally used to study intracellular molecular dynamics. In live cell microscopic imaging there is always exists a compromise between image quality and cell viability. The prerequisite to image rapidly and in numerous dimensions, to capture dynamic intracellular procedures also constrains illumination and exposure regimes and requires fast camera readout. This in turn results in low signal-to-noise ratio (SNR) fluorescence images with mixed Poisson–Gaussian noise. Under such conditions effective denoising techniques are indispensable and become a critical tool to improve quantitative investigation of these images in order to understand dynamic intracellular processes and their fundamental mechanisms. Low illumination conditions generate arbitrary variations in the photon emission and detection process that manifest as Poisson noise in the captured images [1]. Successful denoising algorithms are consequently indispensable before visualization and analysis of these images.

In this paper main aim of the work is to establish the impact of various standards denoising strategies on fluorescence images [2]. Photon and camera readout noises in general degrade fluorescence images. Thus the stochastic data representation is a Mixed-Poisson-Gaussian (MPG) procedure. Therefore consider strategies which moreover work on the Poisson noise or Gaussianize the Poisson process and then denoise the Gaussianized image [3]. For Gaussianizing the images were carried out to variance stabilizing transform (VST) and applied to Anscombe root

transformation $f: z \rightarrow 2\sqrt{z + \frac{3}{8}}$ to the data which determination of Gaussianize the noise which is then removed using a conventional denoising algorithm for additive white Gaussian noise, which in our case is Fuzzy-Shrink using DT-DWT, An inverse transformation is used to estimate the signal of interest for denoised signal.

Proper inverse transformation is primary in order to reduce the bias error which prone position when the nonlinear forward transformation is performed [4]. In [5] developed an algebraic inverse and the asymptotically unbiased inverse that together show the way to a substantial bias at low counts. In this paper, an efficient approach is proposed to determine the impact of various standards of denoising approach on fluorescence images. In this paper, we model the intra-scale dependency in wavelet transform domain as a fuzzy feature. We always postulate that noise is uncorrelated in the spatial domain; it is also uncorrelated in the wavelet domain. With respect to this principle, we use a fuzzy feature for single channel image denoising to enhance image information in wavelet sub-bands, and then using a fuzzy membership function to shrink wavelet coefficients, accordingly. This feature space distinguishes between important coefficients, which belong to image discontinuity and noisy coefficients.

The rest of the paper is organized as follows: Section 2 introduces about Poisson noise, variance stabilization, Gaussian and Poisson denoising along with the conventional inverses of the Anscombe transformation. Section 4 discusses the various experiments, and consists of results followed by conclusion in Section 5.

2. THEORY

2.1. Poisson noise

Let z_i , where $i = 1, \dots, N$, be the experiential pixel values attained through an image acquisition device. Consider each z_i to be an autonomous random Poisson variable whose mean $y_i \geq 0$ is the fundamental intensity value to be calculated. The discrete Poisson probability of each z_i is

$$E\{z_i|y_i\} = \frac{y_i^{z_i} e^{-y_i}}{z_i!} \tag{1}$$

In addition to that the mean of the Poisson variable z_i and the parameter y_i also its variance is as follows:

$$E\{z_i|y_i\} = y_i = \text{var}\{z_i|y_i\} \tag{2}$$

Poisson noise can be defined as

$$\eta_i = z_i - E\{z_i|y_i\} \tag{3}$$

Hence, slightly have $E\{\eta_i|y_i\} = 0$ and $\text{var}\{\eta_i|y_i\} = \text{var}\{z_i|y_i\} = y_i$. As the variance of noise varies the accurate intensity value varies; Poisson noise is depends on signal. In general the standard deviation of the noise η_i equals $\sqrt{y_i}$. Due to this, the effect of Poisson noise increases that is the signal-to-noise ratio decreases as the intensity value decreases.

2.2. Variance stabilization and the Anscombe transformation

The fundamental reason for proposing a VST is to eliminate the dependent data of the noise variance, as a result that it becomes stable for the entire data $z_i, i = 1, \dots, N$. Furthermore, if the transformation is also Gaussian noise distribution, to calculate the intensity values y_i with a conventional denoising method considered for preservative white Gaussian noise. Neither exact stabilization nor exact normalization is probable so, put into practice, an approximate or asymptotical results are employed.

Variance stabilizing transformations is the Anscombe transformation is widely used transform is explained in [6].

$$f: z \rightarrow 2\sqrt{z + \frac{3}{8}} \tag{4}$$

Poisson distributed data gives a signal whose noise is asymptotically additive standard normal by applying (4).

The $f(z)$ is a denosing produces a signal D that can be considered as an estimation of $E\{f(z)|y\}$.

3. IMAGE ENHANCEMENT USING FUZZY SHRINK DT-DWT

In this paper, proposed an efficient technique to enhance the fluorescence image using a new wavelet based fuzzy shrink and thresholding method. The following section discusses about the structural design and the use of fuzzy shrink in fluorescence image enhancement. Initially, the fluorescence images are transformed to preprocessing process for preliminary enhancement. Then the output of preprocessing is given as input to the DT-DWT. In this transform, the preprocessing is not used as the initial step, although it is more efficient. Because it enhances the image contrast by transforming the pixel distribution as a result they can conform to uniform distribution. In this proposed work, the input image which consists of noise is called noisy image is first transformed into wavelet domain. In the wavelet domain there are mainly three processes in which the image first compute the DUAL TREE discrete wavelet transform (DT-DWT), pixel values are converted into wavelet coefficients then decomposed into six sub bands.

After applying wavelet transform small coefficients are subjected by noise, while coefficients with a large absolute value carry more signal information than noise. Replacing the smallest, noisy coefficients by zero and a backwards wavelet transform on the result may lead to a reconstruction with the essential signal characteristics and with less noise. For thresholding three observations and assumptions:

1. The decorrelating property of a wavelet transform creates a sparse signal: most untouched coefficients are zero or close to zero.
2. Noise is spread out equally over all coefficients.
3. The noise level is not too high, so that can recognize the signal and the signal wavelet coefficients.

So, choosing of threshold level is an important task the coefficients having magnitude greater than threshold are considered as signal of interest and keep the same or modified according to type of threshold selected and other coefficients become zero. The image is reconstructed from the modified coefficients. This process is also known as the inverse discrete wavelet transforms (IDWT). Selection of threshold is an important point of interest. Care should be taken so as to preserve the edges of the denoised image. There will be various methods for wavelet thresholding, which depend on the choice of a threshold value. To choose the threshold value using fuzzy shrink rule, finally all the images are summed to low sub-band at the next to finer scale. The process is repeated until the image is reconstructed, at last get enhanced fluorescence image.

3.1 Denoising and Thresholding

Here the denoising is done through Fuzzy shrinkage rule. In image denoising, where a trade-off between noise suppression and the maintenance of actual image discontinuity must be made, solutions are required to detect important image details and accordingly adapt the degree of noise smoothing. With respect to this principle, use a fuzzy feature for single channel image denoising to enhance image information in wavelet sub-bands and then using a fuzzy membership function to shrink wavelet coefficients, accordingly.

3.2 Fuzzy Feature

Here, want to give large weights to neighboring coefficients with similar magnitude, and a small weight to neighboring coefficients with dissimilar magnitude. The larger coefficients are produced by noises which are always isolated or unconnected, but edge coefficients are clustered and persistent. It is well known that the more adjacent points are more similar in magnitude. So use a fuzzy function $m(l, k)$ of magnitude similarity and a fuzzy function $s(l, k)$ of spatial similarity, which is defined as:

$$m(l, k) = \exp \left(- \left(\frac{Y_{s,d}(i, j) - Y_{sd}(i + 1, j + k)}{Thr} \right)^2 \right)$$

Where $Y_{s,d}(i, j)$ and $Y_{sd}(i + 1, j + k)$ are central coefficient and neighbor coefficients in the wavelet sub-bands, respectively. $Thr = c \times \hat{\sigma}_n$, $3 \leq c \leq 4$, $\hat{\sigma}_n$ is estimated noise variance, and N is the number of coefficients in the local window $k \in [-K, \dots, K]$, and $l \in [-L, \dots, L]$. According the two fuzzy functions can get adaptive weight $w(l, k)$ for each neighboring coefficient:

$$w(l, k) = m(l, k) \times s(l, k)$$

Using the adaptive weights, obtain the fuzzy feature for each coefficient in the wavelet sub-bands as follows:

$$f(i, j) = \frac{\sum_{l=-L}^L \sum_{k=-K}^K W(l, k) \times |Y_{sd}(i + 1, j + k)|}{\sum_{l=-L}^L \sum_{k=-K}^K W(l, k)}$$

3.3 Fuzzy Shrinkage Rule

The second step is want to give large weights to neighboring coefficients with similar magnitude, and a small weight to neighboring coefficients with dissimilar magnitude. The next step in the wavelet denoising procedure usually consists of shrinking the wavelet coefficients: the coefficients that contain primarily noise should be reduced to tiny values, while the ones containing a significant noise-free components should be reduced less. Here, use a fuzzy rule based on the fuzzy feature for shrinking the wavelet coefficients. Fuzzy logic was proposed [7], and has application in a large number of fields. The fuzzy sets and fuzzy rules form the knowledge base of a fuzzy rule-based reasoning system. Fuzzy rules are linguistic IF-THEN constructions that have the general form "IF A THEN B", where A and B are (collections of) propositions containing linguistic variables. The variable A is called the premise or antecedent and B is the consequence of the rule [8]. After finding the fuzzy feature, will form Linguistic IF-THEN rules for shrinking wavelet coefficients as follows:

IF the fuzzy feature $f(i, j)$ is large THEN shrinkage of wavelet coefficients $Y_{s,d}(i, j)$ is small.

In fact, the fuzzy feature indicates how coefficients in the noisy sub-band should be shrunk. Fuzzy membership function (MF) is a curve that defines how each point in the input space is mapped to a membership value (or degree of

membership) between 0 and 1. MF is often given the designation of μ . The input space is sometimes referred to as the universe of discourse, a fancy name for a simple concept. The only condition a membership function must really satisfy is that it must vary between 0 and 1. The function itself can bear arbitrary curves whose shape can be defined as a function that suits us from the point of view of simplicity, convenience, speed and efficiency. MF is built from several basic functions such as: piece-wise linear functions, the sigmoid curve, quadratic curve, the Gaussian distribution function and cubic polynomial curves.

A cubic B-spline is a piecewise cubic polynomial that is twice continuously differentiable. This B-spline using here is the second order B-spline membership function and the general equation for unity is termed as

$$\sum_{i=-m}^N B_{i,m}(x) = 1, x_0 \leq x \leq x_n$$

where $m=0,1,2,3,\dots$. Generally, the B-spline basis functions with order higher than 1 are not a normal fuzzy set, in other words, the maximum value of the B-spline membership function does not reach 1. Usually fuzzy systems theory requires that the membership functions are normal, this can be resolved by multiplying the B-spline basis functions by a positive number so that its maximum value is 1. In this paper using B-spline curve to get a smooth joint need to control the position and the curvature at the end points of the curve segments. These curves are highly flexible in nature than the S curves. Here, the B-spline curve is used in which is a mapping on the vector x , and is named because of its B-shape. The parameters T_1 and T_2 locate the extremes of the sloped portion of the curve as given by:

$$\mu(x) = \begin{cases} 0 & x \leq T_1 \\ 2X \left(\frac{x - T_1}{T_2 - T_1} \right)^2 & T_1 \leq x \leq \frac{T_1 + T_2}{2} \\ 1 - 2 \left(T_2 - \frac{x}{T_2 - T_1} \right)^2 & \frac{T_1 + T_2}{2} \leq x \leq T_2 \\ 1 & x \geq T_2 \end{cases}$$

Here, also drawn an S shaped curve [8] by using the mapping on the vector x , and is named because of its S shape. By using the above parameters of the T_1 and T_2 the spline based curve also drawn with the B-Spline curve. Finally, the estimated noise-free signal is obtained using the following formula:

$$\hat{X}_{s,d}(i, j) = \mu(f(i, j) \times Y_{s,d}(i, j))$$

For building fuzzy membership function, two thresholds (T_1 and T_2), must be determined. Hence, found out that T_1 and T_2 are related with the $\hat{\sigma}_n$ which is the estimated noise variance. In order to find these relations, we have done some experiments using test images. We found out that T_1 and T_2 have nonlinear

relation with the $\hat{\sigma}_n$. For achieving the nonlinear relation, have to test the noise reduction algorithm with the different noisy images. In each different noise variance, the result obtained best values for T1 and T2.

$$T_1 = K_1 \times \hat{\sigma}_n$$

$$T_2 = K_2 \times \hat{\sigma}_n$$

Where k_1 and the k_2 are the constant values. $\hat{\sigma}_n$ is the noise variance using median estimator.

$$\hat{\sigma}_n = \frac{1}{N - 1} \sum_{i=1}^N (x_i - \bar{x})^2$$

Where x_i is the selected pixels, \bar{x} is the centered pixels and the N is the order of samples using this noise variance of the image is calculated.

Indeed, this method is a simple fuzzy IFTHEN rule, which assigns smaller local window and smaller level of decomposition when the estimated noise variance is small, and vice versa then the denoising output of the image is given to the inverse of the DWT for the reconstruction of the image. Then the image is sent for post processing process.

3.4. Post Processing

Processing is usually result from a modification of the spatial correlation between wavelet coefficients (often caused by zeroing of small neighboring coefficients) or by using DWT. DWT is shift invariance and will cause some visual artifacts in thresholding based denoising. For this reason, the fuzzy filter is used on the results of the proposed fuzzy-shrink algorithm to reduce artifacts to some extent. First, use a window of size $(2L+1) \times (2K+1)$ centered at (i, j) to filter the current image pixel at position (i, j) . Next, the similarity of neighboring pixels to the center pixel is calculated. Adaptive weight $w(l, k)$ for each neighboring coefficient is calculated. Finally, the output of post-processing step is determined as follows:

$$\tilde{x}(i, j, c) = \frac{\sum_{l=-L}^L \sum_{k=-K}^K w(l, k) \times \hat{x}(i + 1, j + k, c)}{\sum_{l=-L}^L \sum_{k=-K}^K w(l, k)}$$

Where, \hat{x} is the denoised image, which can be obtained using proposed fuzzy-shrink algorithm. After the post processing process the enhanced leaf image is obtained as a result.

4. EXPERIMENTS

The experiments mainly consist of following steps as the forward Anscombe transformation to noisy images, and then denoise the transformed image with Fuzzy-

Shrink using DT-DWT [9], lastly the inverse transform is applied to get a final enhanced image. Evaluate the performance by peak signal-to-noise ratio (PSNR). The PSNR is calculated as

$$10 \log_{10} \left(\frac{\max(y_i)^2}{\sum_i ((\hat{y}_i - y_i)^2 | N)} \right)$$

Where N is the total number of pixels in the image.

The test images taken for the experiment is shown in **Figure 1a, 1b and 1c** and the performance of the proposed approach is evaluated in terms of PSNR.

Table II shows the results using Fuzzy-Shrink using DT-DWT. The plots of the PSNR values obtained using BLS_GSM and Fuzzy-Shrink using DT-DWT shows that DT-DWT provides higher SNR for low count image when the sigma value is low. As the sigma value increases there is a steep fall in the signal to noise ratio. For higher count images, the ISNR is less in Fuzzy-Shrink using DT-DWT when compared with the BLS-GSM technique. The results are tabulated in Table.1.

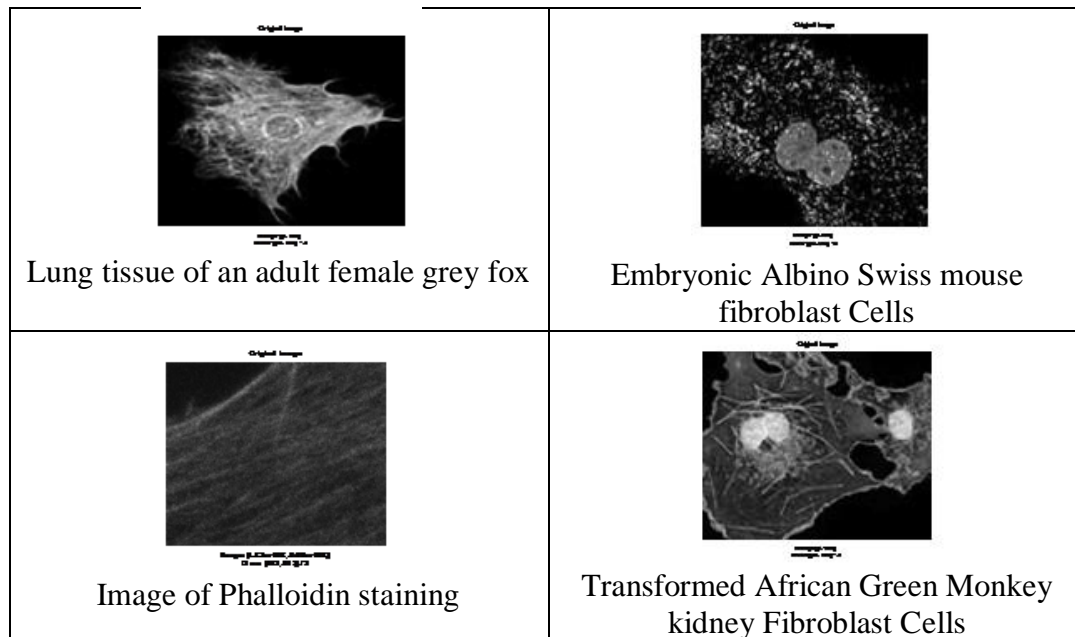
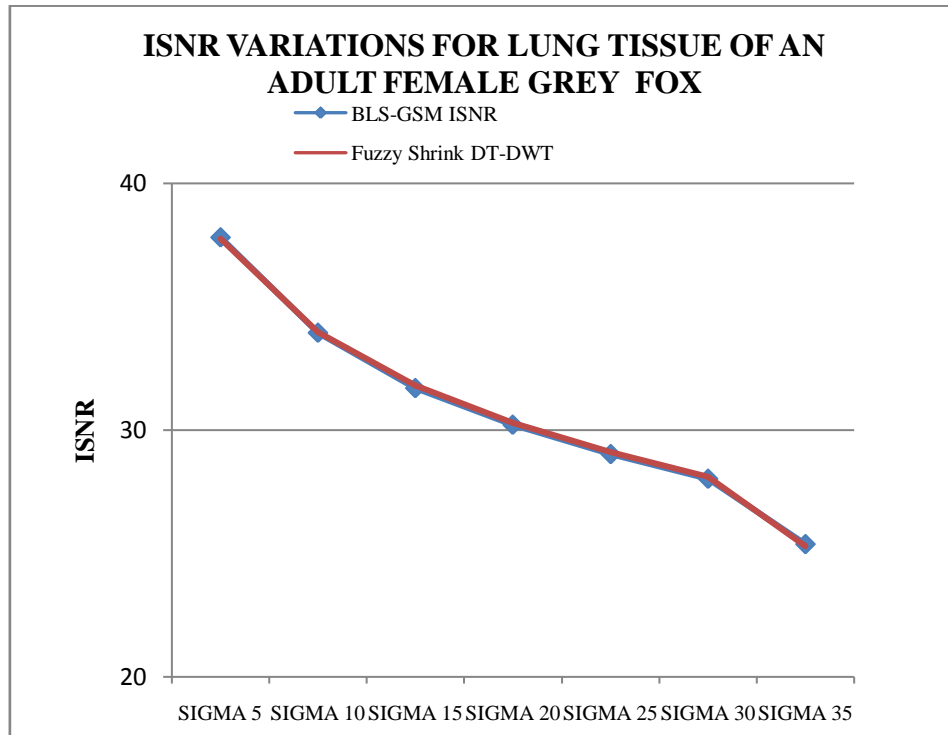


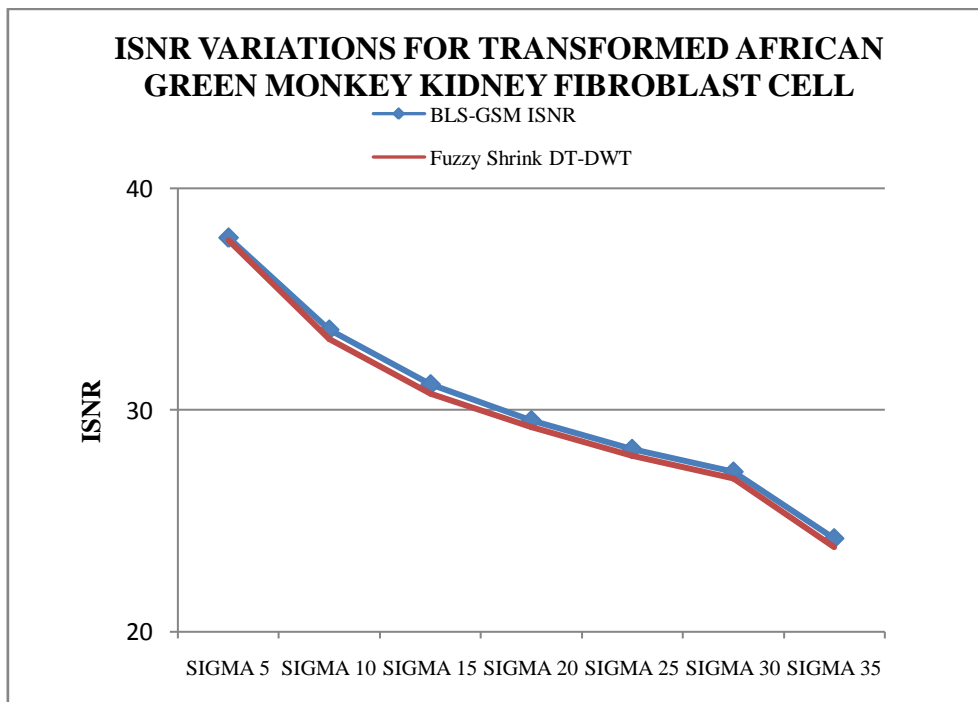
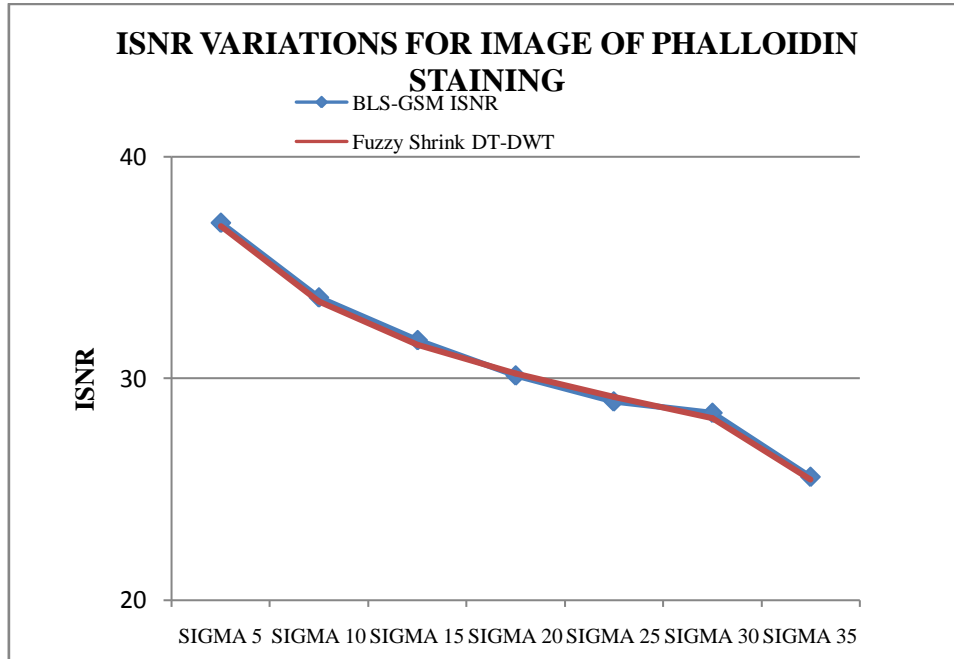
Figure 1: The Four Test Images used in the Experiments

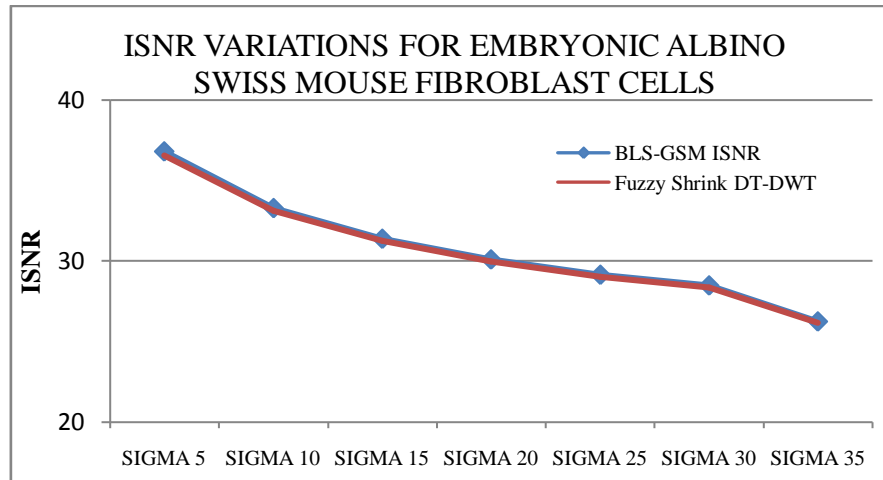
Table 1: Test Results using Fuzzy-Shrink using DT-DWT

IMAGES	FIGURE 1(a)		FIGURE 1(b)		FIGURE 1(c)		FIGURE 1(d)	
	ISNR WITH ASYMPTOTIC INVERSE	ISNR WITH FUZZY-SHRI NK USING DT-DWT	ISNR WITH ASYMPTOTIC INVERSE	ISNR WITH FUZZY-SHRI NK USING DT-DWT	ISNR WITH ASYMPTOTIC INVERSE	ISNR WITH FUZZY-SHRI NK USING DT-DWT	ISNR WITH ASYMPTOTIC INVERSE	ISNR WITH FUZZY-SHRI NK USING DT-DWT
σ_n 5	37.81	37.75	37.02	36.89	37.77	37.65	36.82	36.56
10	33.96	33.99	33.67	33.49	33.63	33.21	33.29	33.14
15	31.72	31.81	31.75	31.53	31.17	30.75	31.37	31.25
20	30.22	30.31	30.13	30.24	29.55	29.24	30.11	29.96
25	29.04	29.11	28.96	29.18	28.26	27.96	29.16	29.03
30	28.04	28.11	28.46	28.21	27.22	26.91	28.47	28.35
35	25.38	25.31	25.56	25.45	24.21	23.83	26.23	26.15

Result Plot Variations







5. CONCLUSION

In this paper, we use a new wavelet-based multi-channel image denoising using intra-scale dependency as a fuzzy feature, and inter-channel relation to improve wavelet coefficients' information at the shrinkage step. We use the DT-DWT for wavelet analysis, because it is shift invariant, and has more directional sub-bands compared to the DWT. In other words, proposing a new method for shrinking wavelet coefficients in the second step of the wavelet-based image denoising is the main novelty of this paper. The comparison of the denoising results obtained with our algorithm, and with the best state-of-the-art methods, demonstrate the performance of our fuzzy approach, which gave the best output PSNRs for most of the images. In addition, the visual quality of our denoised images exhibits the fewest number of artifacts and preserves most of edges compared to other methods.

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